

## English Version



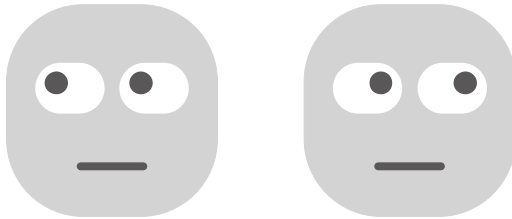
### Exercise 5B



#### Fundamental Questions

1. In each of the following, determine whether the pair of plane figures are congruent by observation.

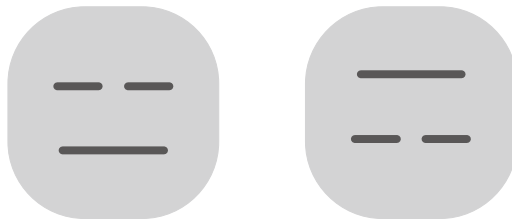
(a)



(b)

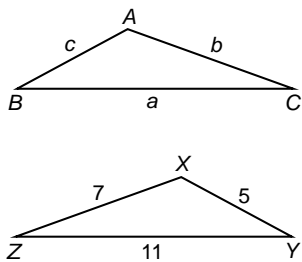


(c)

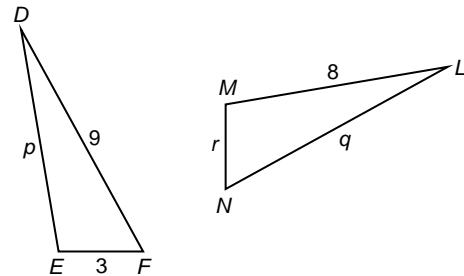


Find the unknowns in each of the following. (2 – 9)

2.  $\triangle ABC \cong \triangle XYZ$

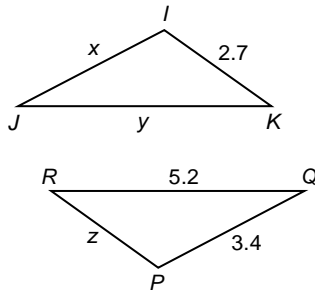


3.  $\triangle DEF \cong \triangle LMN$

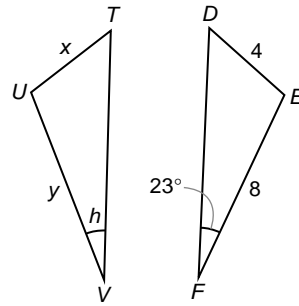
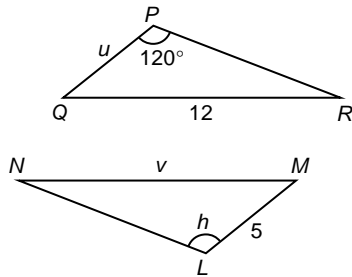


4.  $\triangle IJK \cong \triangle PQR$

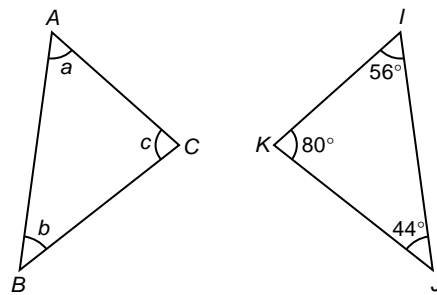
5.  $\triangle TUV \cong \triangle DEF$



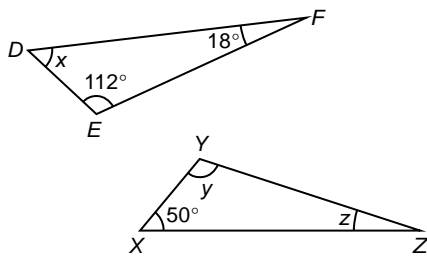
6.  $\triangle PQR \cong \triangle LMN$



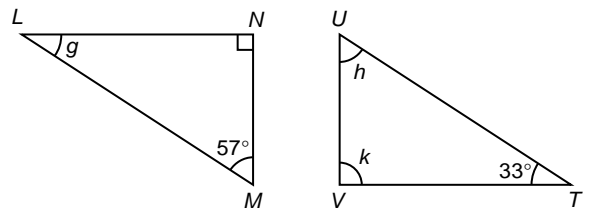
7.  $\triangle ABC \cong \triangle IJK$



8.  $\triangle DEF \cong \triangle XYZ$



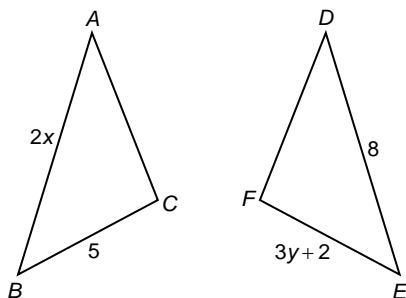
9.  $\triangle LMN \cong \triangle TUV$



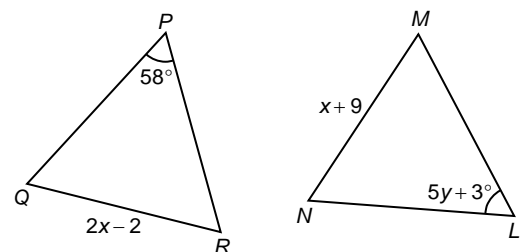
### Consolidation Questions

Find the unknowns in each of the following. (10 – 15)

10.  $\triangle ABC \cong \triangle DEF$

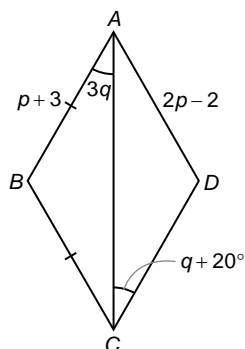


11.  $\triangle PQR \cong \triangle LMN$

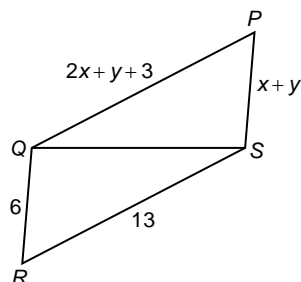
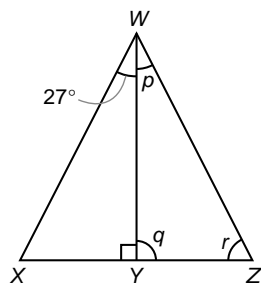


12.  $\triangle ABC \cong \triangle ADC$

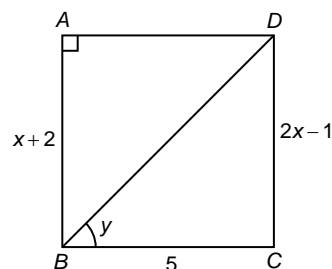
13.  $\triangle PQS \cong \triangle RSQ$



14.  $\triangle WXY \cong \triangle WZY$

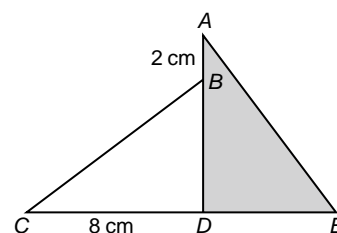


15.  $\triangle ABD \cong \triangle CDB$



16. In the figure,  $ABD$  is a straight line and  $D$  is the foot of perpendicular from  $A$  to  $CE$ . If  $\triangle BCD \cong \triangle EAD$ ,

- (a) find the length of  $DE$ ,  
 (b) find the area of  $\triangle ADE$ .



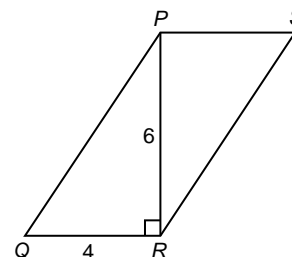
### Challenging Questions

17. It is given that  $\triangle LMN \cong \triangle XYZ$ . If  $XY = 7$ ,  $\angle MLN = 42^\circ$  and  $\angle XYZ = 38^\circ$ ,

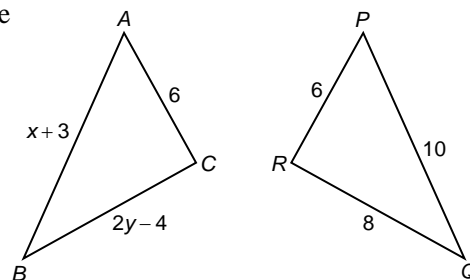
- (a) find the length of  $LM$ ,  
 (b) find  $\angle XZY$ .

18. In the figure,  $\triangle PQR \cong \triangle RSP$ .

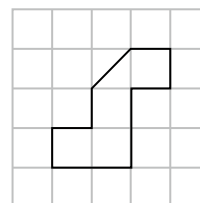
- (a) Find the length of  $PS$ .  
 ★(b) A rectangular coordinate system, with  $R$  as the origin, is introduced such that  $QR$  lies on the negative  $x$ -axis,  $PR$  lies on the positive  $y$ -axis and the coordinates of  $Q$  are  $(-4, 0)$ .  
 (i) Write down the coordinates of  $P$  and  $S$ .  
 (ii) If  $\triangle TPS \cong \triangle RSP$ , write down the possible coordinates of  $T$ .



19. The figure shows two congruent triangles. Find all possible sets of values of  $x$  and  $y$ .



20. (a) Divide the figure into 3 congruent figures.  
 (b) If the figure can be divided into  $n$  congruent triangles, find the least number of  $n$ .



## Exercise 5C

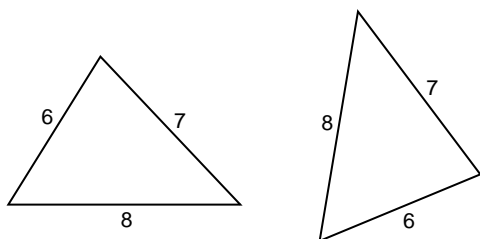
[The figures in this exercise may not be drawn to scale.]



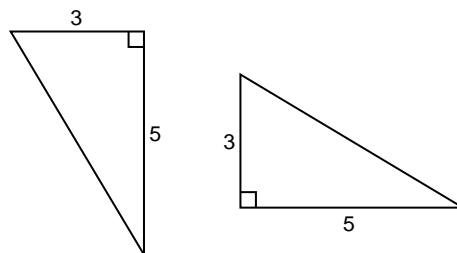
### Fundamental Questions

In each of the following, two congruent triangles are given. State the reason for each pair of congruent triangles. (1 – 2)

1.

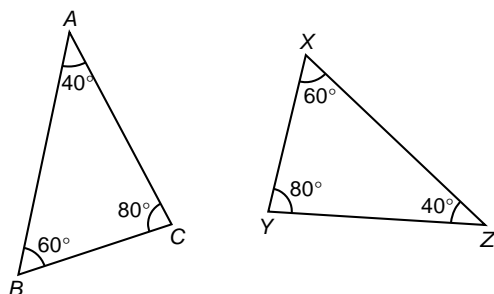


2.

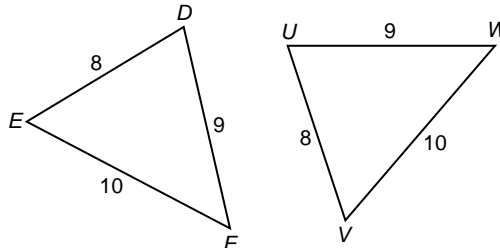


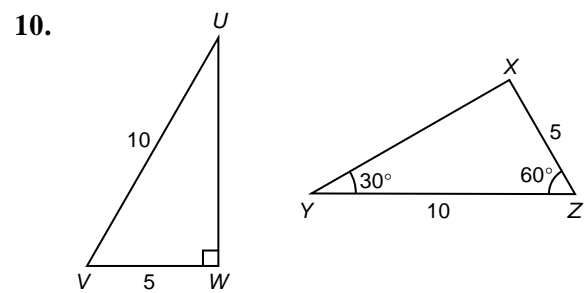
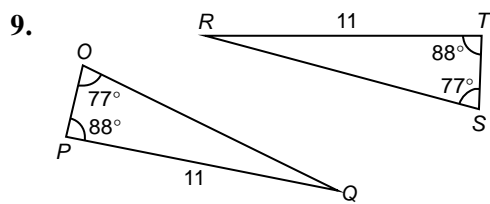
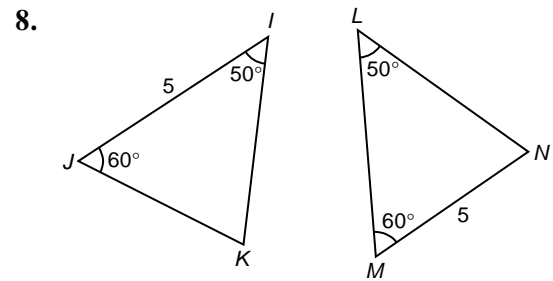
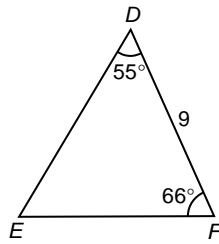
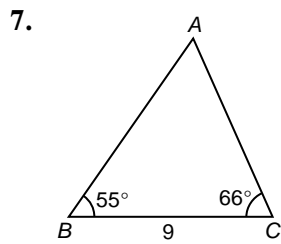
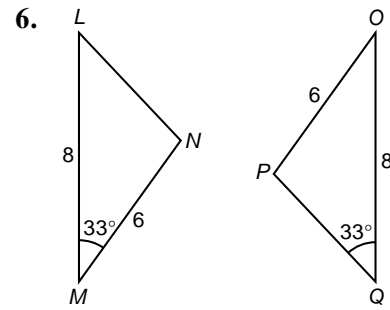
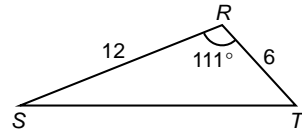
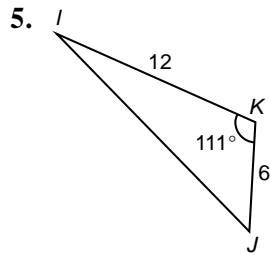
Determine whether each of the following pairs of triangles must be congruent. If they are, write down the pair of congruent triangles and give the reason. (3 – 10)

3.



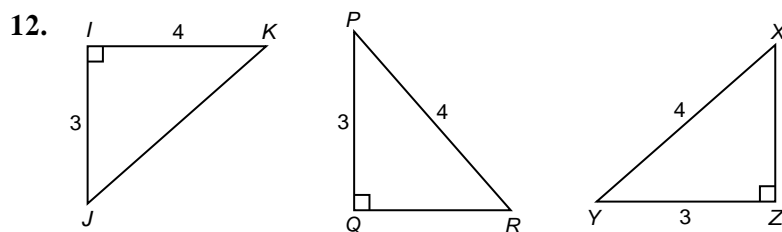
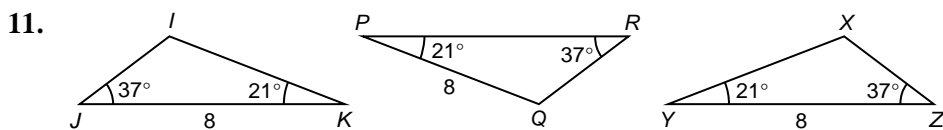
4.



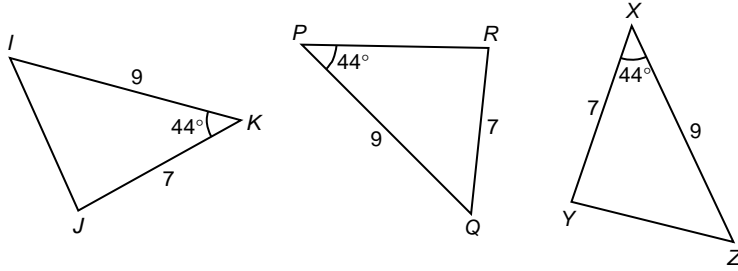


### Consolidation Questions

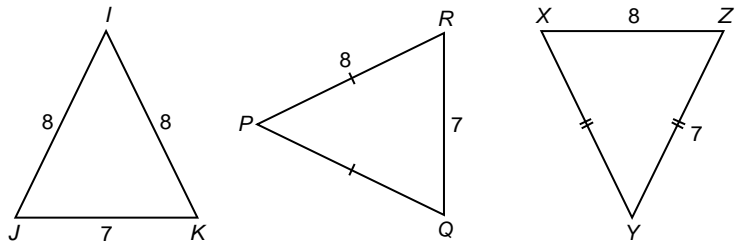
In each of the following, which triangles must be congruent? Give the reason. (11 – 15)



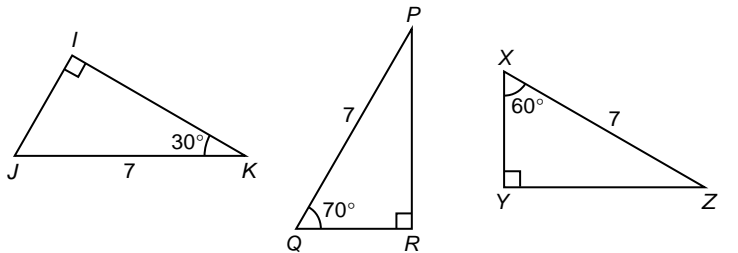
13.



14.



15.



For each of the following, determine whether  $\triangle ABC$  must have only one possible size and shape. (16 – 20)

16.  $AB = 6$  cm,  $BC = 5$  cm,  $CA = 7$  cm

17.  $BC = 11$  cm,  $\angle BAC = 88^\circ$ ,  $\angle ACB = 22^\circ$

18.  $AB = 9$  cm,  $BC = 7$  cm,  $\angle ABC = 90^\circ$

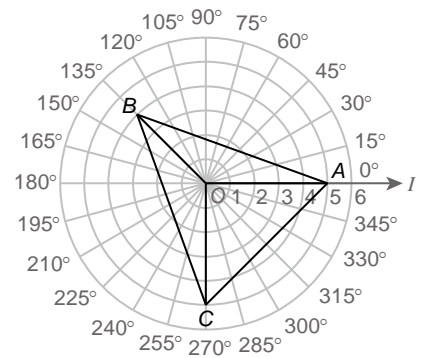
19.  $\angle BAC = 77^\circ$ ,  $\angle ABC = 52^\circ$ ,  $\angle ACB = 51^\circ$

20.  $AC = 9$  cm,  $\angle BAC = 111^\circ$ ,  $\angle ACB = 22^\circ$



### Challenging Questions

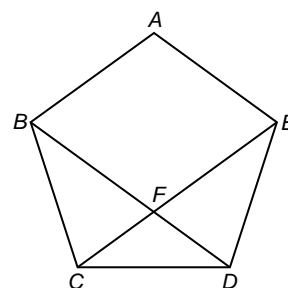
21. (a) Find the lengths of  $OA$ ,  $OB$  and  $OC$ .  
 (b) Find  $\angle AOB$  and  $\angle BOC$ .  
 (c) Write down a pair of congruent triangles and give the reason.



22.  $A(0, 7)$  is rotated anticlockwise about the origin  $O$  through

$90^\circ$  to  $B$ .  $C$  is the reflection image of  $B$  with respect to the  $y$ -axis.

- Write down the coordinates of  $B$  and  $C$ .
  - Find the lengths of  $OB$  and  $OC$ .
  - Write down a pair of congruent triangles and give the reason.
  - Billy claims that  $\triangle ABC$  is an isosceles triangle. Do you agree? Explain your answer.
23. In the figure,  $ABCDE$  is a regular pentagon.  $BD$  and  $CE$  intersect at  $F$ .
- Are  $\triangle BCD$  and  $\triangle EDC$  congruent? If they are, give the reason.
  - Write down another pair of congruent triangles.



## Exercise 5D

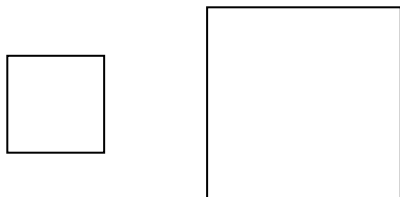
[The figures in this exercise may not be drawn to scale.]



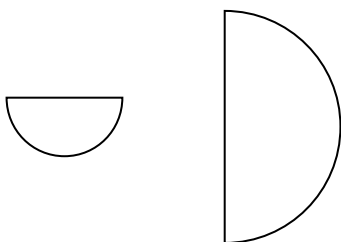
### Fundamental Questions

1. In each of the following, determine whether the pair of plane figures are similar by observation.

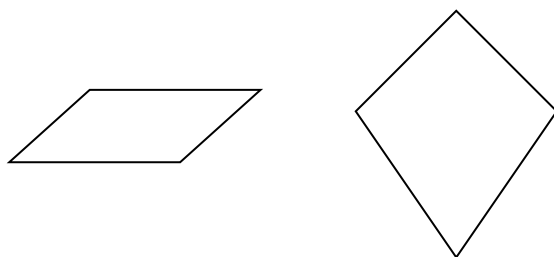
(a)



(b)



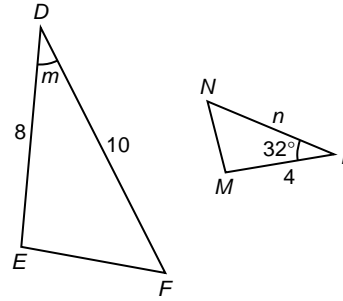
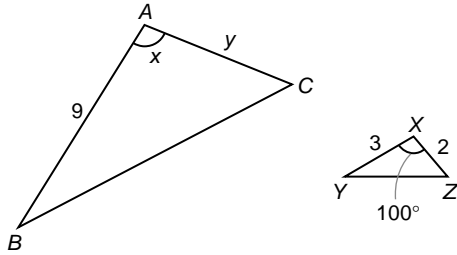
(c)



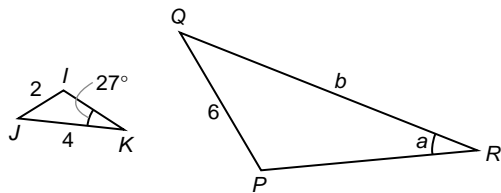
Find the unknowns in each of the following. (2 – 7)

2.  $\triangle ABC \sim \triangle XYZ$

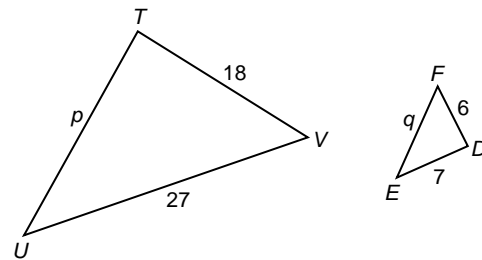
3.  $\triangle DEF \sim \triangle LMN$



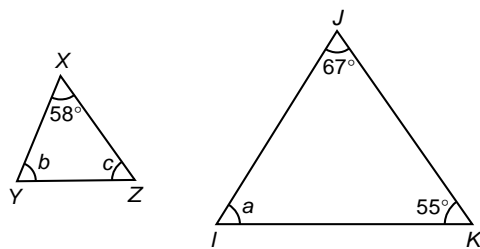
4.  $\triangle IJK \sim \triangle PQR$



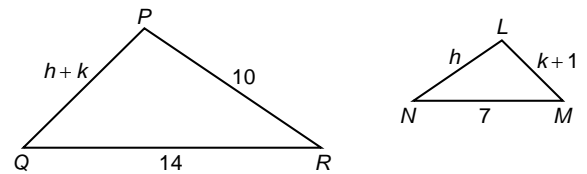
5.  $\triangle TUV \sim \triangle DEF$



6.  $\triangle XYZ \sim \triangle IJK$

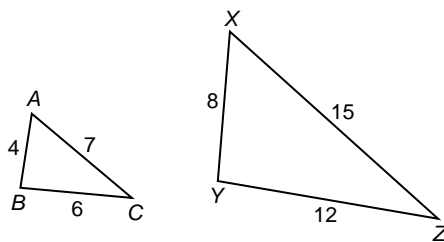


7.  $\triangle PQR \sim \triangle LMN$

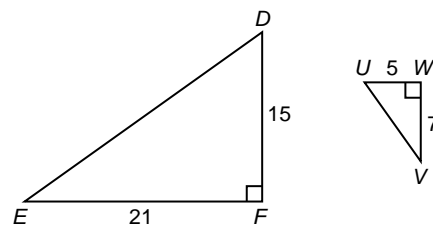


Determine whether each of the following pairs of triangles must be similar. If they are, write down the pair of similar triangles and give the reason. (8 – 11)

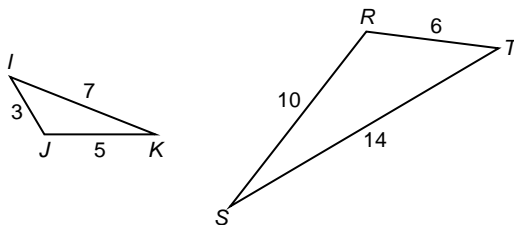
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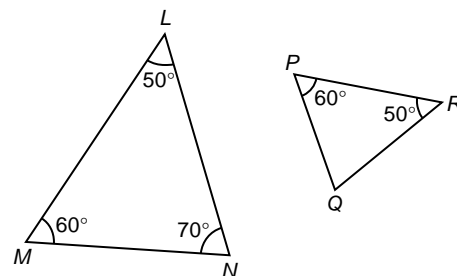
9.



10.



11.



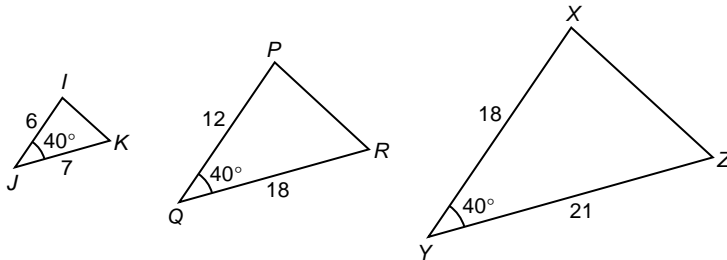




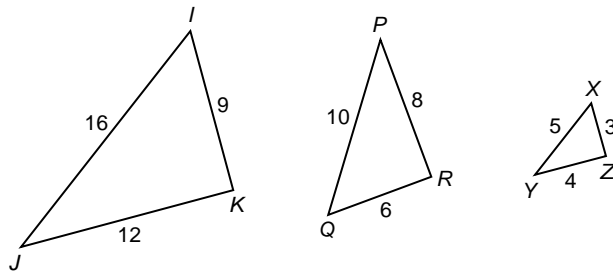
### Consolidation Questions

In each of the following, which triangles must be similar? Give the reason. (12 – 14)

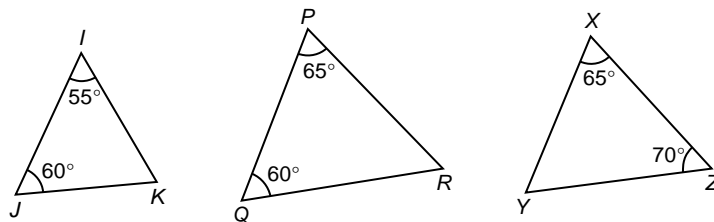
12.



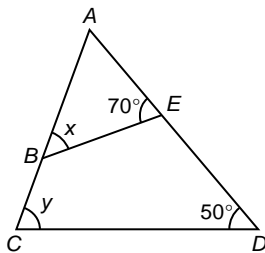
13.



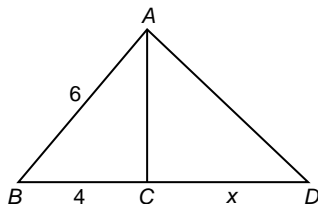
14.



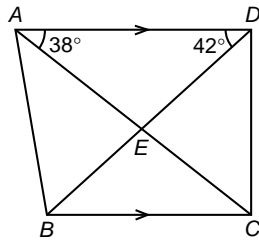
15. In the figure,  $ABC$  and  $AED$  are straight lines. If  $\triangle ABE \sim \triangle ADC$ , find  $x$  and  $y$ .



16. In the figure,  $BCD$  is a straight line. If  $\triangle ABC \sim \triangle DBA$ , find  $x$ .

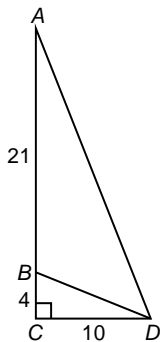


17. In the figure,  $ABCD$  is a trapezium, where  $AD \parallel BC$ .  $AC$  and  $BD$  intersect at  $E$ .



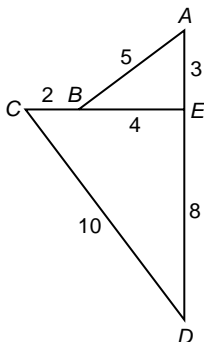
- (a) Find  $\angle ACB$  and  $\angle CBD$ .
- (b) Write down a pair of similar triangles and give the reason.

18. In the figure,  $ABC$  is a straight line.



- (a) Are  $\triangle ACD$  and  $\triangle DCB$  similar? If they are, give the reason.
- ★ (b) Emma claims that  $BD$  is shorter than half of  $AD$ . Do you agree? Explain your answer.

19. In the figure,  $AED$  and  $CBE$  are straight lines.

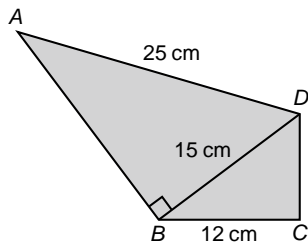


- (a) Are  $\triangle ABE$  and  $\triangle CDE$  similar? If they are, give the reason.
- (b) Find  $\angle AEB$ .

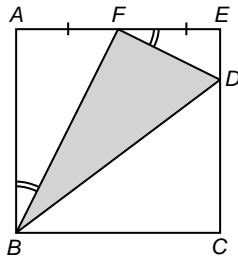
### Challenging Questions

20. It is given that  $\triangle ABC \sim \triangle XYZ$ . If  $AB = AC$  and  $\angle YXZ = 50^\circ$ , find  $\angle XYZ$ .

21. In the figure,  $\triangle ABD \sim \triangle BCD$ . Find the area of  $ABCD$ .



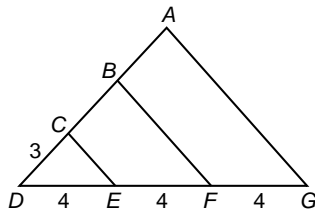
22. In the figure, the perimeter of the square  $ABCE$  is 64 cm.  $D$  and  $F$  are points lying on  $CE$  and  $AE$  respectively.



- (a) Write down a pair of similar triangles and give the reason.  
 (b) Find the area of  $\triangle BDF$ .



23. In the figure,  $ABCD$  and  $DEFG$  are straight lines. It is given that  $\triangle ADG \sim \triangle BDF \sim \triangle CDE$ .



- (a) Do  $DE$ ,  $DF$  and  $DG$  form an arithmetic sequence? Explain your answer.  
 (b) Do  $DC$ ,  $DB$  and  $DA$  form an arithmetic sequence? Explain your answer.


**Exercise 5B** (page 5.2)

1. (a) Yes (b) No (c) Yes
2.  $a=11$ ,  $b=7$ ,  $c=5$
3.  $p=8$ ,  $q=9$ ,  $r=3$
4.  $x=3.4$ ,  $y=5.2$ ,  $z=2.7$
5.  $h=23^\circ$ ,  $x=4$ ,  $y=8$
6.  $h=120^\circ$ ,  $u=5$ ,  $v=12$
7.  $a=56^\circ$ ,  $b=44^\circ$ ,  $c=80^\circ$
8.  $x=50^\circ$ ,  $y=112^\circ$ ,  $z=18^\circ$
9.  $g=33^\circ$ ,  $h=57^\circ$ ,  $k=90^\circ$
10.  $x=4$ ,  $y=1$
11.  $x=11$ ,  $y=11^\circ$
12.  $p=5$ ,  $q=10^\circ$
13.  $x=4$ ,  $y=2$
14.  $p=27^\circ$ ,  $q=90^\circ$ ,  $r=63^\circ$
15.  $x=3$ ,  $y=45^\circ$
16. (a) 6 cm (b)  $24\text{ cm}^2$
17. (a) 7 (b)  $100^\circ$
18. (a) 4  
(b) (i)  $P(0, 6)$ ,  $S(4, 6)$   
(ii)  $(4, 0)$ ,  $(4, 12)$
19.  $x=7$ ,  $y=6$  or  $x=5$ ,  $y=7$
20. (b) 9

**Exercise 5C** (page 5.6)

1. S.S.S.
2. S.A.S.
3. No
4. Yes;  $\triangle DEF \cong \triangle UVW$  (S.S.S.)
5. Yes;  $\triangle IJK \cong \triangle STR$  (S.A.S.)
6. No
7. Yes;  $\triangle ABC \cong \triangle EDF$  (A.S.A.)
8. No
9. Yes;  $\triangle OPQ \cong \triangle STR$  (A.A.S.)
10. Yes;  $\triangle UVW \cong \triangle YZX$  (R.H.S.)
11.  $\triangle IJK \cong \triangle XZY$  (A.S.A.)

12.  $\triangle PQR \cong \triangle YZX$  (R.H.S.)
13.  $\triangle IJK \cong \triangle ZYX$  (S.A.S.)
14.  $\triangle IJK \cong \triangle PQR$  (S.S.S.)  
or  $\triangle IJK \cong \triangle PRQ$  (S.S.S.)
15.  $\triangle IJK \cong \triangle YXZ$  (A.S.A.)  
or  $\triangle IJK \cong \triangle YXZ$  (A.A.S.)
16. Yes
17. Yes
18. Yes
19. No
20. Yes
21. (a)  $OA=5$  units,  $OB=4$  units,  $OC=5$  units  
(b)  $\angle AOB=135^\circ$ ,  $\angle BOC=135^\circ$   
(c)  $\triangle OAB \cong \triangle OCB$  (S.A.S.)
22. (a)  $B(-7, 0)$ ,  $C(7, 0)$   
(b)  $OB=7$  units,  $OC=7$  units  
(c)  $\triangle AOB \cong \triangle AOC$  (S.A.S.)  
or  $\triangle AOB \cong \triangle COA$  (S.A.S.)  
(d) Yes
23. (a) Yes;  $\triangle BCD \cong \triangle EDC$  (S.A.S.)  
(b)  $\triangle BCF \cong \triangle EDF$

**Exercise 5D** (page 5.9)

1. (a) Yes  
(b) Yes  
(c) No
2.  $x=100^\circ$ ,  $y=6$
3.  $m=32^\circ$ ,  $n=5$
4.  $a=27^\circ$ ,  $b=12$
5.  $p=21$ ,  $q=9$
6.  $a=58^\circ$ ,  $b=67^\circ$ ,  $c=55^\circ$
7.  $h=5$ ,  $k=3$
8. No
9. Yes;  $\triangle DEF \sim \triangle UVW$  (ratio of 2 sides, inc.  $\angle$ )
10. Yes;  $\triangle IJK \sim \triangle TRS$  (3 sides proportional)
11. Yes;  $\triangle LMN \sim \triangle RPQ$  (A.A.A.)
12.  $\triangle IJK \sim \triangle XYZ$  (ratio of 2 sides, inc.  $\angle$ )
13.  $\triangle PQR \sim \triangle YXZ$  (3 sides proportional)
14.  $\triangle IJK \sim \triangle RQP$  (A.A.A.)
15.  $x=50^\circ$ ,  $y=70^\circ$
16. 5
17. (a)  $\angle ACB=38^\circ$ ,  $\angle CBD=42^\circ$   
(b)  $\triangle AED \sim \triangle CEB$  (A.A.A.)
18. (a) Yes; ratio of 2 sides, inc.  $\angle$

**(b)** Yes

**19. (a)** Yes; 3 sides proportional

**(b)**  $90^\circ$

**20.**  $65^\circ$

**21.**  $204\text{ cm}^2$

**22. (a)**  $\triangle ABF \sim \triangle EFD$  (A.A.A.)

**(b)**  $80\text{ cm}^2$

**23. (a)** Yes

**(b)** Yes

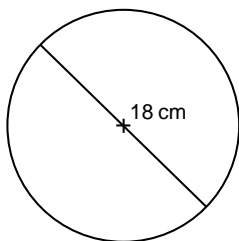
**English Version****10 Mensuration****Exercise 10A**

[In this exercise, unless otherwise stated, give your answers correct to 1 decimal place if necessary.]

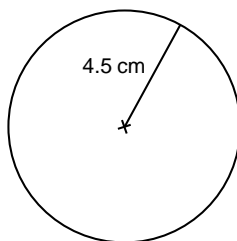
**Fundamental Questions**

Find the circumference of each of the following circles. (1 – 2)

1.



2.



3. Find the circumference of each of the following circles.

(a) A circle of diameter 35 cm (Take  $\pi = 3.14$ .)

(b) A circle of radius 19.6 cm (Take  $\pi = \frac{22}{7}$ .)

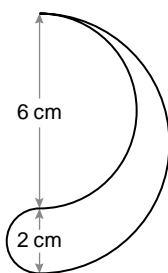
4. If the circumference of a circle is 75.36 m, find the radius of the circle. (Take  $\pi = 3.14$ .)

5. The circumference of a circular plate is 44 cm. Find the diameter of the plate. (Take  $\pi = \frac{22}{7}$ .)

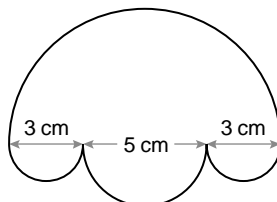
**Consolidation Questions**

The following figures are formed by semi-circles. Find the perimeter of each figure. (Express your answers in terms of  $\pi$ .) (6 – 8)

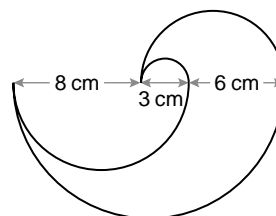
6.



7.



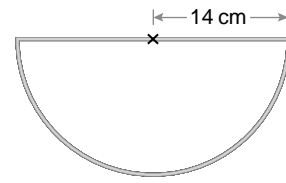
8.



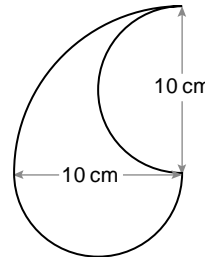
9. A rope of 198 cm long is used to surround the circular base of a can 6 times. Find the diameter of the base of the can.

10. The tip of the hour hand of a clock moves 100.48 cm in a day. Find the length of the hour hand.  
(Take  $\pi = 3.14$ .)

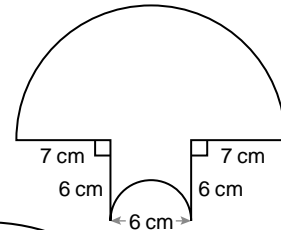
11. Judy bends a wire into a semi-circle of radius 14 cm. Find the length of the wire.



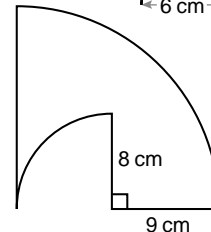
12. The figure is formed by a quadrant and semi-circles. Find the perimeter of the figure.



13. The figure is formed by semi-circles and straight lines. Find the perimeter of the figure.



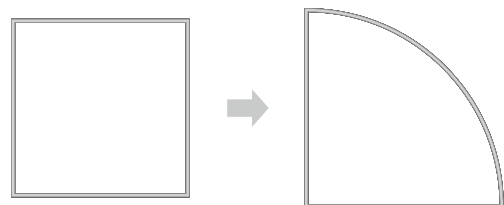
14. The figure is formed by quadrants and straight lines. Find the perimeter of the figure.



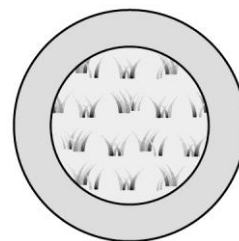
15. The ratio of the circumferences of two circles is 5 : 3. What is the ratio of their radii?
16. The diameter of a car wheel is 48 cm. If the wheel makes 550 revolutions per minute, find the speed of the car in km/h.
17. The radius of a bicycle wheel is 0.3 m. If Eva rides the bicycle at a constant speed of 10 km/h for 20 minutes, how many revolutions does the wheel make? (Give your answer correct to the nearest integer.)

### Challenging Questions

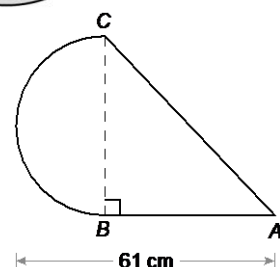
18. In the figure, the square is formed by a wire and its area is  $484 \text{ cm}^2$ .
- (a) Find the length of the wire.
- (b) If the wire is bent into a quadrant, find the radius of the quadrant.



19. In the figure, a circular lawn is surrounded by a path of uniform width. The difference between the circumferences of the lawn and the outer edge of the path is 11 m. Find the width of the path. (Give your answer correct to 3 significant figures.)



20. The figure is formed by a semi-circle and a right-angled



triangle  $ABC$ .  $AB : BC = 20 : 21$ .

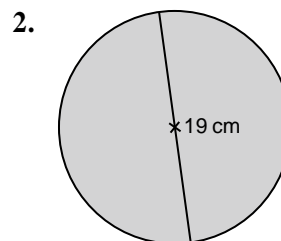
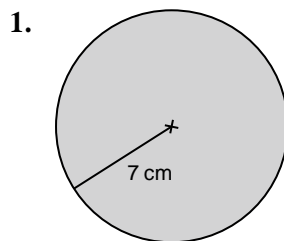
- Find the radius of the semi-circle.
- Find the perimeter of the figure.

## Exercise 10B

[In this exercise, unless otherwise stated, give your answers correct to 1 decimal place if necessary.]

### Fundamental Questions

Find the area of each of the following circles. (1 – 2)



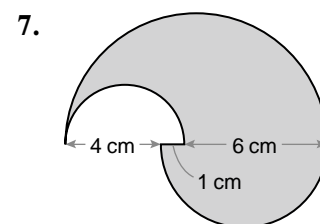
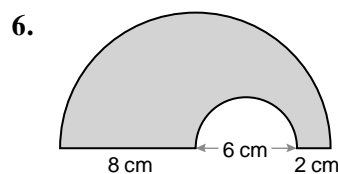
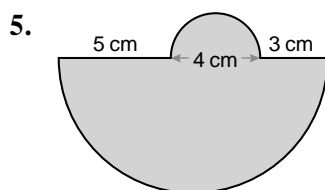
3. Find the area of each of the following circles.

- A circle of radius 15 cm (Take  $\pi = 3.14$ .)
- A circle of diameter 25.2 cm (Take  $\pi = \frac{22}{7}$ .)

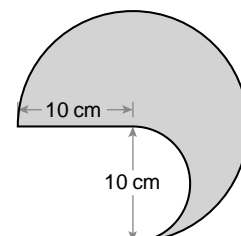
4. The area of a discus is  $350 \text{ cm}^2$ . Find the radius of the discus.

### Consolidation Questions

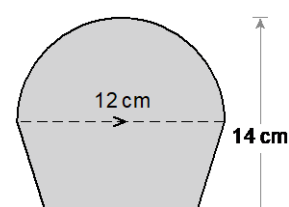
The following figures are formed by semi-circles and straight lines. Find the area of each figure. (Express your answers in terms of  $\pi$ .) (5 – 7)



- The circumference of a circular flying disc is 75 cm. Find the area of the flying disc.
- A circular farm of area  $42 \text{ m}^2$  is surrounded by a fence. Find the length of the fence.
- The figure is formed by a quadrant, semi-circles and a straight line. Find the area of the figure.



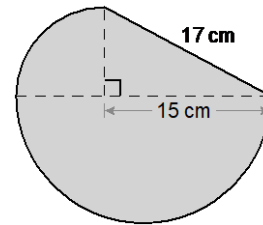
- The figure is formed by a semi-circle and straight lines. Find the



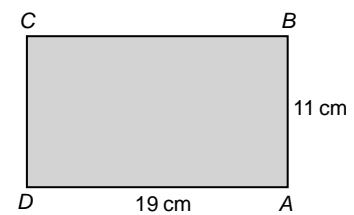


area of the figure.

12. The figure is formed by a quadrant, a semi-circle and a straight line. Find the area of the figure.

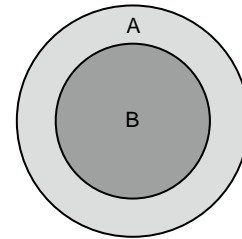


13. Daisy wants to cut the largest circle from the rectangular cardboard  $ABCD$  as shown in the figure. Find the area of the circle obtained by Daisy.



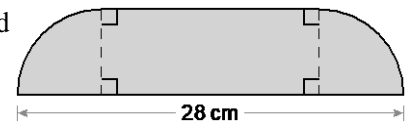
14. The figure consists of two concentric circles. The ratio of the radius of the inner circle to that of the outer circle is  $2 : 3$ . The circumference of the inner circle is  $12\pi$  cm.

- (a) Find the radius of the outer circle.  
(b) What is the difference between the areas of region A and region B? (Express your answer in terms of  $\pi$ .)



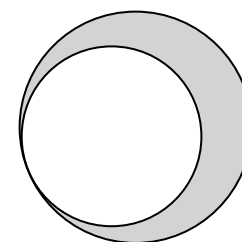
15. The figure is formed by two quadrants of radii  $r$  cm each and straight lines. The perimeter of the figure is 63 cm.

- (a) Find the value of  $r$ .  
(b) Find the area of the figure.

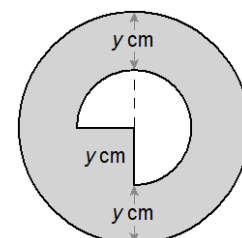


16. In the figure, the ratio of the radii of two circles is  $7 : 9$ .

- (a) Find the ratio of the area of the smaller circle to that of the larger circle.  
(b) If the area of the shaded region is  $48\text{ cm}^2$ , find the area of the smaller circle.

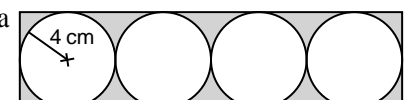


17. The figure is formed by a circle, three identical quadrants and straight lines. If the area of the shaded region is  $273\text{ cm}^2$ , find the value of  $y$ .



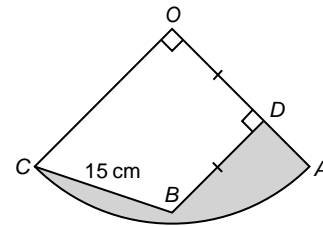
### Challenging Questions

18. In the figure, four circles of radii 4 cm each is enclosed by a rectangle. Find the area of the shaded region.



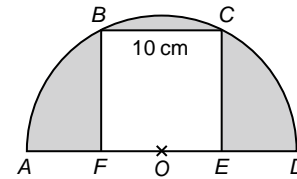
19. The figure shows a quadrant.  $D$  is a point lying on  $OA$  such that  $OA \perp BD$  and  $OD = BD = 2AD$ .  $BC = 15$  cm.

- (a) Find the length of  $OC$ .  
(b) Find the area of the shaded region.



20. In the figure,  $ABCD$  is a semi-circle with centre  $O$ .  $E$  and  $F$  are points lying on  $AD$ . The length of the side of square  $BCEF$  is 10 cm.  $OE = OF$ .

- (a) Find the radius of the semi-circle.  
(b) What percentage of the figure is shaded?



21. The difference between the radii of two circles is 10 cm and the difference between the areas of these two circles is  $660 \text{ cm}^2$ .

- (a) Find the sum of the radii of two circles.  
(b) Find the radii of two circles.  
(c) Howard claims that the sum of the areas of two circles is greater than  $900 \text{ cm}^2$ . Do you agree? Explain your answer.

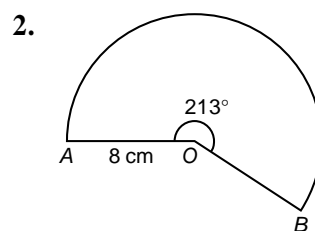
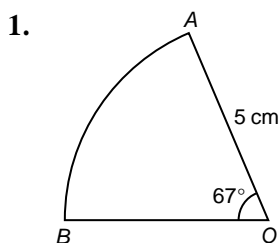
(Express your answers in terms of  $\pi$  if necessary.)

## Exercise 10C

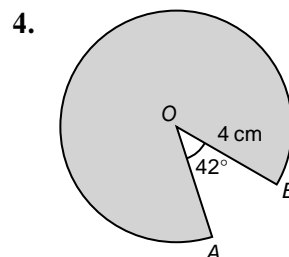
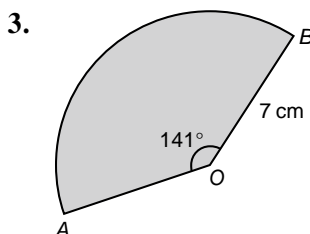
[In this exercise, unless otherwise stated, give your answers correct to 3 significant figures if necessary.]

### Fundamental Questions

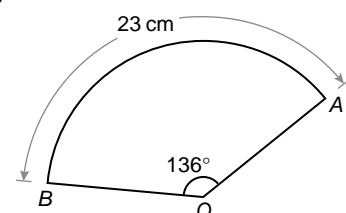
In each of the following figures, find the length of  $\widehat{AB}$ . (1 – 2)



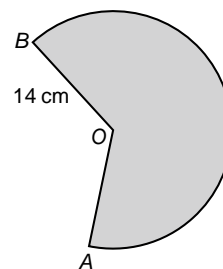
In each of the following figures, find the area of sector  $AOB$ . (3 – 4)



5. In the figure, the length of  $\widehat{AB}$  is 23 cm and  $\angle AOB = 136^\circ$ . Find the radius of the sector.

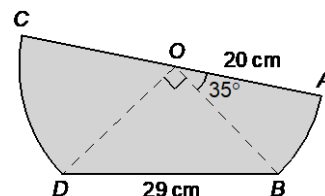


6. In the figure, the area of sector  $AOB$  is  $400 \text{ cm}^2$ . Find the angle at the centre of the sector.

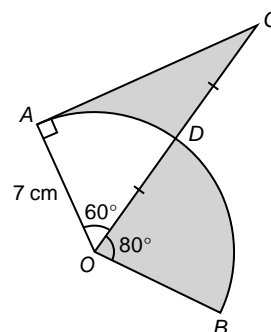
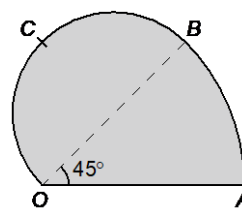


### Consolidation Questions

7. The angle at the centre and the area of a sector are  $125^\circ$  and  $50\pi \text{ cm}^2$  respectively.
- Find the radius of the sector.
  - Find the perimeter of the sector.
8. The arc length and the area of a sector are  $10\pi \text{ cm}$  and  $30\pi \text{ cm}^2$  respectively.
- Find the radius of the sector.
  - Find the angle at the centre of the sector.
9. The figure is formed by  $\triangle OBD$ , sector  $OAB$  and sector  $OCD$ .  $AOC$  is a straight line.
- Find the length of  $OD$ .
  - Find the area of the figure.
10. A sector is formed by a wire of  $70 \text{ cm}$  long and the angle at the centre of the sector is  $48^\circ$ .
- Find the radius of the sector.
  - If the wire is bent into a new sector and the radius of the new sector is half of that obtained in (a), find the angle at the centre of the new sector.

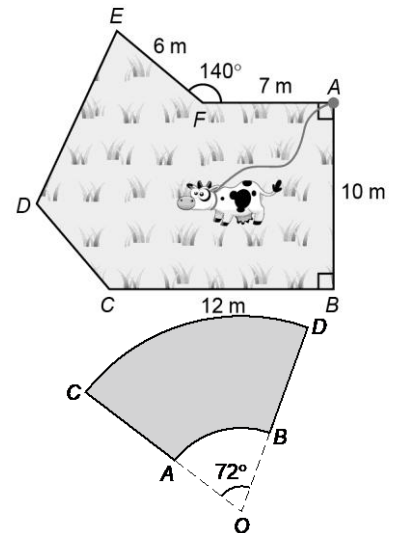


11. In the figure,  $OAB$  is a sector and  $OCB$  is a semi-circle. The perimeter of the figure is  $65 \text{ cm}$ .
- Find the length of  $OA$ .
  - Find the area of the figure.
12. In the figure,  $OAB$  is a sector.  $OC$  and  $\widehat{AB}$  intersect at  $D$  such that  $OD = DC$ .
- Find the length of  $AC$ .
  - Find the area of the shaded region.



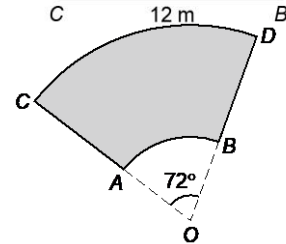
13. The figure shows a piece of grassland  $ABCDEF$ . A cow is tied to the post at  $A$  with a rope. Find the area of grassland that the cow can eat in each of the following situations.

- (a) The rope is 5 m long.  
 (b) The rope is 9 m long.  
 (Ignore the size of the cow in the calculation.)



14. In the figure,  $OAB$  and  $OCD$  are two sectors with centre  $O$ . The perimeter of the shaded region is  $(20\pi + 40)$  cm and  $OA : AC = 3 : 4$ .

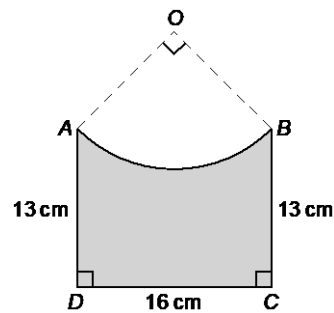
- (a) Find the length of  $OA$ .  
 (b) Find the area of the shaded region in terms of  $\pi$ .



### Challenging Questions

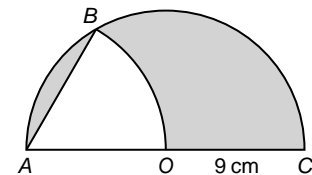
15. In the figure,  $O$  is the centre of sector  $AOB$ .

- (a) Find the length of  $OA$ .  
 (b) Find the perimeter of the shaded region.  
 (c) Find the area of the shaded region.

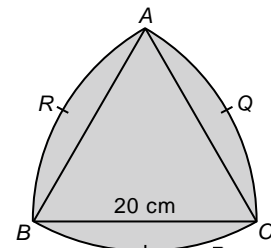


16. In the figure,  $O$  is the centre of semi-circle  $ABC$  and  $A$  is the centre of arc  $OB$ .

- (a) Find the perimeter of the shaded region.  
 (b) Find the area of the shaded region.

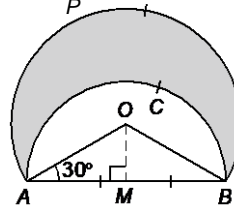


17. In the figure,  $\triangle ABC$  is an equilateral triangle of side 20 cm. The centres of  $\widehat{BPC}$ ,  $\widehat{AQC}$  and  $\widehat{ARB}$  are  $A$ ,  $B$  and  $C$  respectively. Find the area of the shaded region.



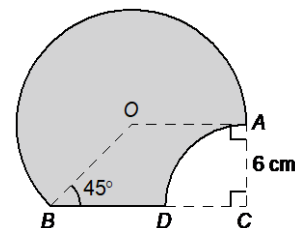
18. In the figure,  $OADB$  is a sector and  $ACB$  is a semi-circle.  $M$  is the mid-point of  $AB$ .  $OM = 5$  cm and  $OA = 10$  cm.

- (a) Find the length of  $AM$ .  
 (b) Find the angle at the centre of sector  $OADB$ .  
 (c) Find the area of the shaded region.



19. In the figure,  $O$  and  $C$  are the centres of sectors  $OAB$  and  $CAD$  respectively.  $BDC$  is a straight line.

- (a) Find the angle at the centre of sector  $OAB$ .  
 (b) Find the length of  $OB$ .  
 (c) Find the perimeter of the shaded region.  
 (d) Find the area of the shaded region.



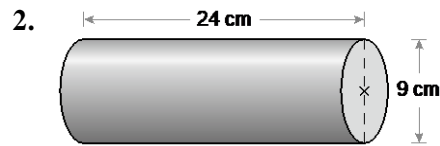
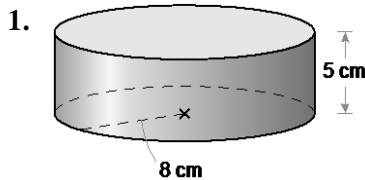


## Exercise 10D

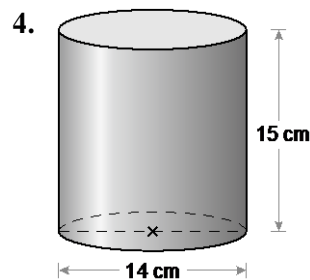
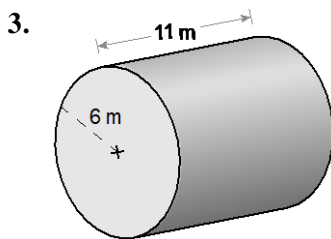
[In this exercise, unless otherwise stated, give your answers correct to 3 significant figures if necessary.]

### Fundamental Questions

Find the volume of each of the following cylinders. (Express your answers in terms of  $\pi$ .) (1 – 2)



Find the total surface area of each of the following cylinders. (Express your answers in terms of  $\pi$ .) (3 – 4)

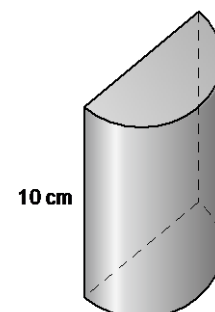


5. The height and the capacity of a cylindrical rubbish bin without a lid are 32 cm and  $2888\pi \text{ cm}^3$  respectively.
  - (a) Find the base radius of the rubbish bin.
  - (b) Find the total surface area of the rubbish bin.
6. The base diameter and the total surface area of a cylinder are 16 cm and  $240\pi \text{ cm}^2$  respectively.
  - (a) Find the height of the cylinder.
  - (b) Find the volume of the cylinder in terms of  $\pi$ .



### Consolidation Questions

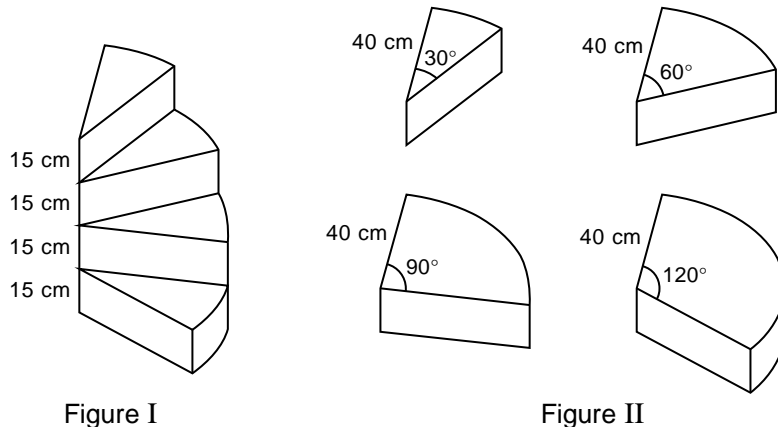
7. The curved surface area of a cylinder is  $110\pi \text{ cm}^2$  and the circumference of its base is  $10\pi \text{ cm}$ .
  - (a) Find the height of the cylinder.
  - (b) Find the volume of the cylinder.
8. In the figure, the uniform cross-section of a solid is a semi-circle and the volume of the solid is  $125\pi \text{ cm}^3$ .
  - (a) Find the base radius of the solid.
  - (b) If the cost of painting the solid is  $\$0.8/\text{cm}^2$ , find the total painting cost.
9. The base diameter and the height of a cylinder are the same. The



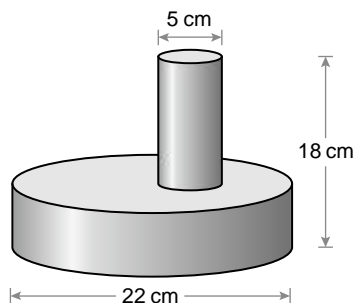
total surface area of the cylinder is  $486\pi \text{ cm}^2$ .

- (a) Find the height of the cylinder.
- (b) Find the volume of the cylinder in terms of  $\pi$ .

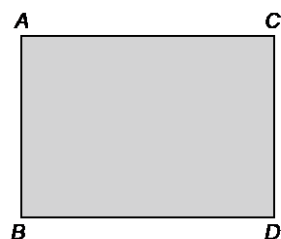
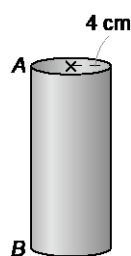
10. A cylindrical container of base radius 5 cm is filled with water of volume  $240 \text{ cm}^3$ . After putting 4 identical weights into the container, the depth of water becomes 4.4 cm. Find the volume of a weight.
11. Figure I shows a spiral staircase formed by 4 steps of height 15 cm each. The uniform cross-section of each step is a sector of radius 40 cm. The angles at the centre of these 4 sectors are  $30^\circ$ ,  $60^\circ$ ,  $90^\circ$  and  $120^\circ$  (see Figure II). Find the volume of the spiral staircase.



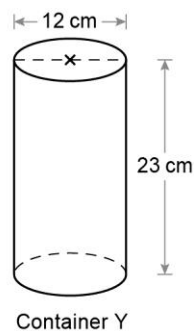
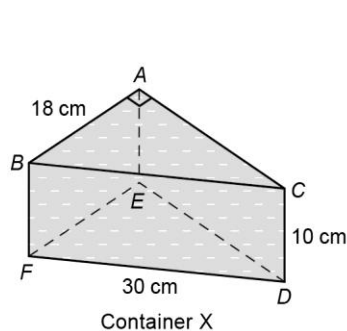
12. The solid in the figure is formed by two cylinders. The base diameters of the upper and the lower cylinders are 5 cm and 22 cm respectively. The height of the solid is 18 cm and the height of the upper cylinder is twice that of the lower cylinder. Find the total surface area of the solid. (Express your answer in terms of  $\pi$ .)



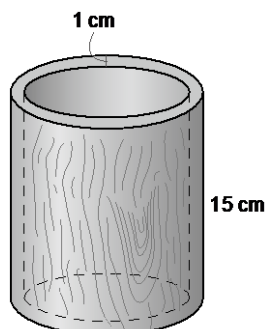
13. A metal cylinder of base radius 5 cm and height 24 cm is melted and recast into 12 smaller identical metal cylinders of height 12.5 cm each.
  - (a) Find the base radius of each smaller metal cylinder.
  - (b) Find the percentage increase in the total surface area of the metal cylinder.
14. Figure I shows a hollow paper cylinder of base radius 4 cm. Its curved surface area is  $144\pi \text{ cm}^2$ .



- (a) Find the height of the hollow cylinder.
- (b) The cylinder is cut along  $AB$  vertically and flattened out to become a rectangular paper (see Figure II). The paper is then rolled up until  $AC$  touches  $BD$ , and two bases are added to form the cylinder in Figure III. Kyle claims that the volume of the cylinder in Figure III is greater than  $630 \text{ cm}^3$ . Do you agree? Explain your answer.



- (a) Find the length of  $AC$ .
- (b) All water in container X is poured into container Y.
- (i) Find the depth of water in container Y.
- (ii) Now,  $n$  marbles of volume  $8 \text{ cm}^3$  each are put into container Y. If the marbles are immersed in water and no water overflows, find the maximum value of  $n$ .



- Find the inner base radius of the cup.
- Find the volume of wood required to make the cup.

17. Figure I shows the uniform cross-section of a container for minced shrimp. It is given that  $O$  is the centre of  $\widehat{ACB}$  and  $\widehat{DFE}$ ,  $OA = OB = 2$  cm,  $AD = BE = 0.5$  cm and  $\angle AOB = 125^\circ$ . The length of the container is 10 cm (see Figure II).

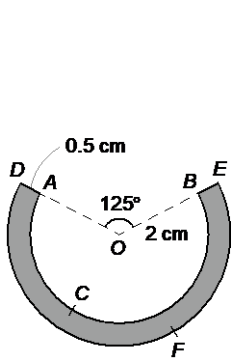


Figure I

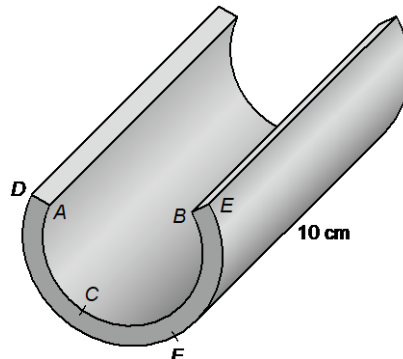
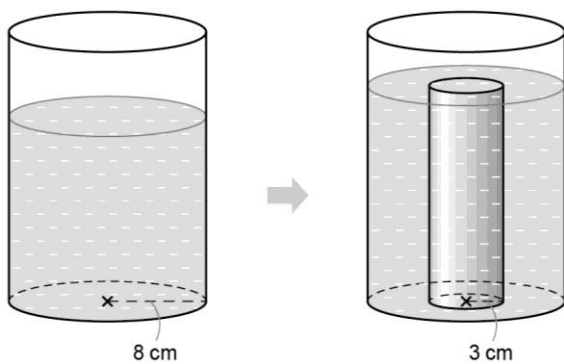
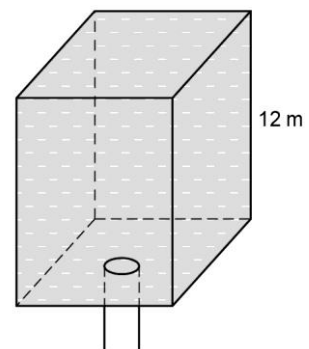


Figure II

- Find the lengths of  $\widehat{ACB}$  and  $\widehat{DFE}$ .
  - Find the total surface area of the container.
18. The figure shows a cylindrical container of base radius 8 cm with some water inside. The total area of the wet surface of the container is  $304\pi$  cm<sup>2</sup>.



- Find the depth of water.
  - A solid cylinder of base radius 3 cm is put into the container vertically and it is just immersed in water. Find the rise in water level.
19. The figure shows a rectangular tank with square base and the tank is fully filled with water. The height and the total area of all lateral surfaces of the tank are 12 m and 432 m<sup>2</sup> respectively.
- Find the length of the side of the base of the tank.
  - A pipe is connected at the bottom of the tank. The cross-section of the pipe is a circle of diameter 40 cm, and the water in the tank is released through the pipe at 0.9 m/s. Find the time required to release all water from the tank. (Give your answer correct to the nearest minute.)



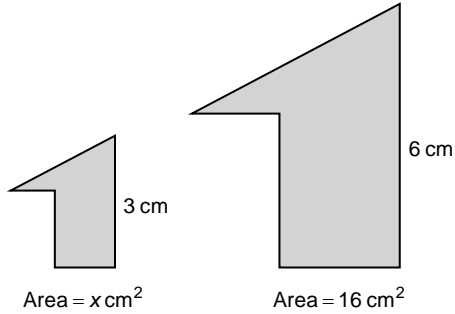


# Exercise 10E

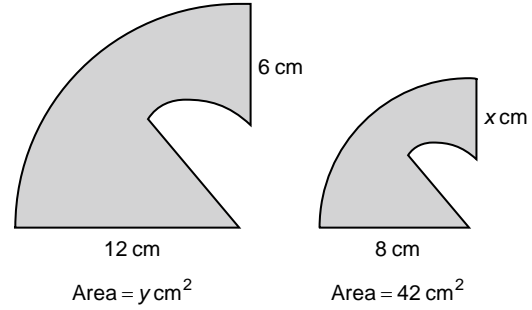
## Fundamental Questions

Find the unknowns in each of the following pairs of similar figures. (1 – 4)

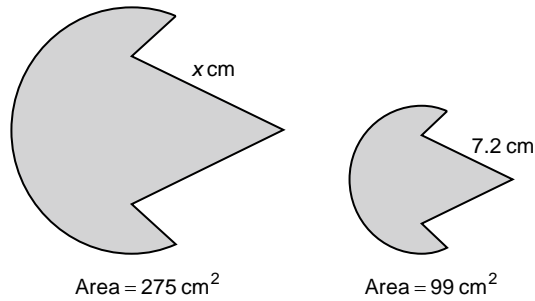
1.



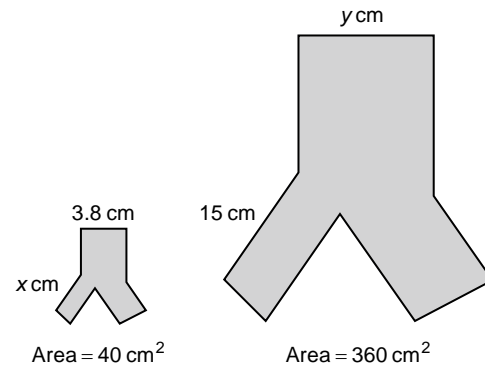
2.



3.

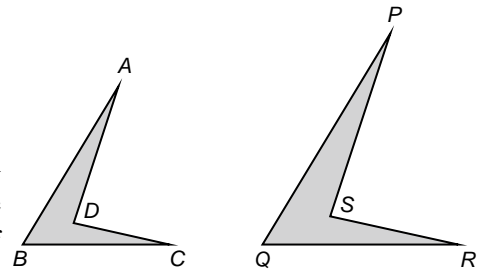


4.

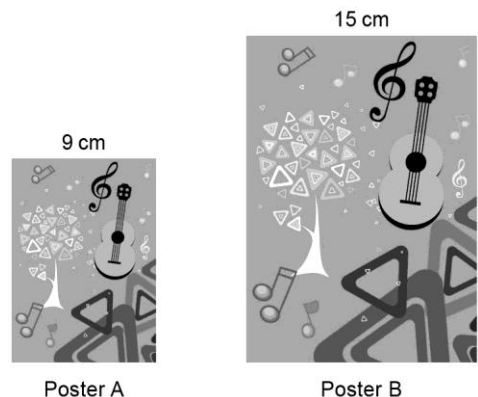


## Consolidation Questions

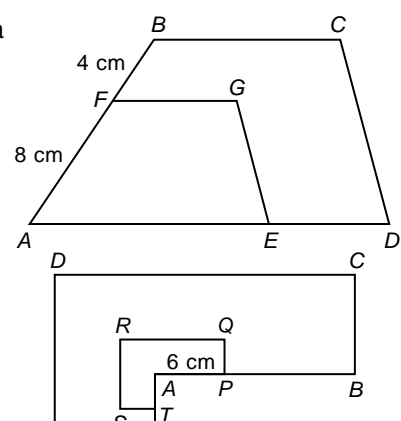
5. The figure shows two similar quadrilaterals  $ABCD$  and  $PQRS$  of perimeters 45 cm and 60 cm respectively. If the area of quadrilateral  $PQRS$  is  $208 \text{ cm}^2$ , find the area of quadrilateral  $ABCD$ .



6. The figure shows two similar posters A and B of widths 9 cm and 15 cm respectively. What is the area of poster A as a percentage of that of poster B?



7. In the figure,  $ABCD$  and  $AFGE$  are two similar figures. If the area of  $AFGE$  is  $56 \text{ cm}^2$ , find the area of  $ABCD$ .

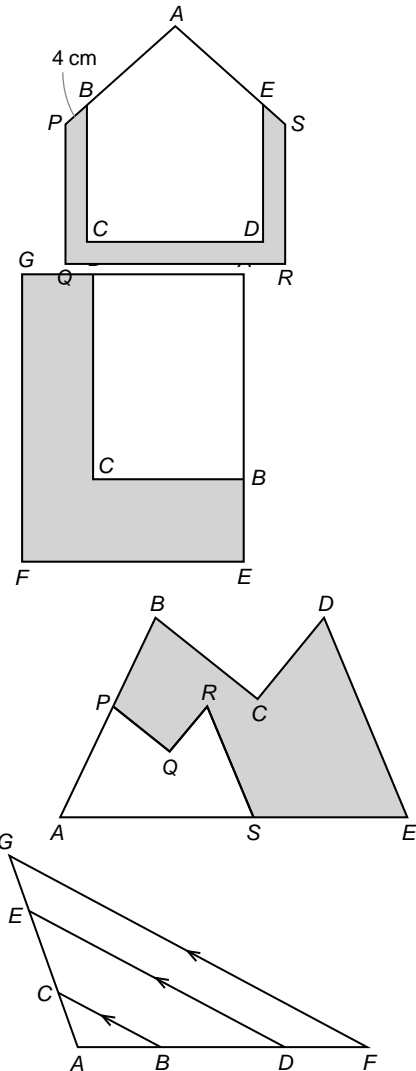


8. In the figure,  $ABCDEF$  and  $APQRST$  are two similar figures. Their areas are  $125 \text{ cm}^2$  and  $20 \text{ cm}^2$  respectively. If  $AP = 6 \text{ cm}$ , find the length of  $PB$ .
9. The scale of the floor plan of a flat is  $1 \text{ cm}$  to  $1.5 \text{ m}$ . If the area of the sitting room on the floor plan is  $8.1 \text{ cm}^2$ , find its actual area.



### Challenging Questions

10. In the figure,  $ABCDE$  and  $APQRS$  are two similar pentagons. The areas of  $ABCDE$  and the shaded region are  $64 \text{ cm}^2$  and  $36 \text{ cm}^2$  respectively. If  $BP = 4 \text{ cm}$ , find the length of  $AB$ .
11. In the figure,  $ABCD$  and  $AEFG$  are two similar rectangles. If the area of the shaded region is  $\frac{24}{25}$  of the area of  $ABCD$ , find  $\frac{AE}{AB}$ .
12. In the figure,  $ABCDE$  and  $APQRS$  are two similar pentagons. It is given that  $AP : PB = 5 : 4$  and the area of the shaded region is larger than that of  $APQRS$  by  $93 \text{ cm}^2$ . Find the area of  $APQRS$ .
13. In the figure,  $AB : AD : AF = 2 : 5 : 7$ . Find the ratio of the area of  $BCED$  to that of  $DEGF$ .

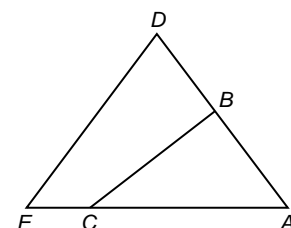


### Exercise 10F



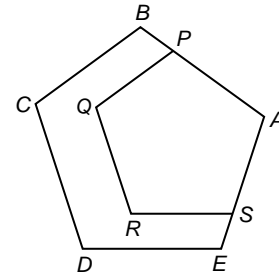
### Fundamental Questions

1. The length and width of a rectangular signboard are measured as  $2.3 \text{ m}$  and  $1.2 \text{ m}$  respectively, correct to 1 decimal place.
- (a) Find the upper limit and lower limit of the length.
- (b) Find the upper limit and lower limit of the width.
2. The figure shows  $\triangle ABC$  and  $\triangle ADE$ . The lengths of  $AB$  and  $BD$  are measured as  $13.6 \text{ cm}$  and  $10.9 \text{ cm}$  respectively, correct to 3 significant figures.
- (a) Find the upper limit and lower limit of  $AB$ .
- (b) Find the upper limit and lower limit of  $BD$ .



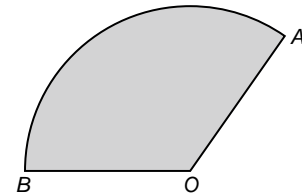
(c) Find the upper limit and lower limit of  $AD$ .

3. The figure shows two pentagons  $ABCDE$  and  $APQRS$ . The lengths of  $AB$  and  $AP$  are measured as 8.47 cm and 6.21 cm respectively, correct to 2 decimal places. Find the possible range of  $PB$ .

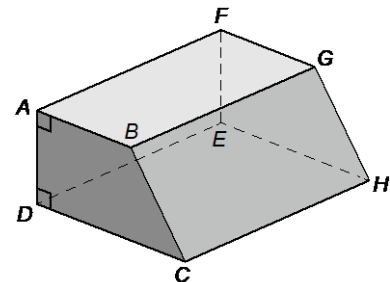


### Consolidation Questions

4. The diameter of a circle is measured as 12 cm, correct to 2 significant figures.
- Find the upper limit and lower limit of the diameter.
  - Find the upper limit and lower limit of the actual area of the circle. (Express your answers in terms of  $\pi$ .)
5. The figure shows sector  $AOB$ . The length of  $OA$  is measured as 14 cm, correct to the nearest cm.  $\angle AOB$  is measured as  $125^\circ$ , correct to the nearest degree.
- Find the upper limit and lower limit of  $OA$ .
  - Find the upper limit and lower limit of  $\angle AOB$ .
  - Find the least possible area of sector  $AOB$ . (Express your answer in terms of  $\pi$ .)



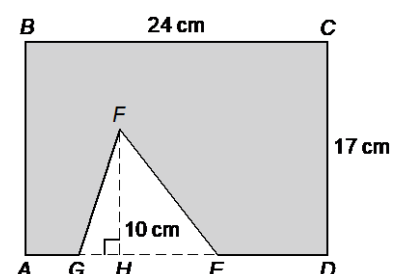
6. The figure shows a right prism. By measurement,  $AB = 2.4$  m,  $AD = 2.2$  m,  $DC = 3.0$  m and  $AF = 3.2$  m, correct to 1 decimal place.
- Find the upper limit and lower limit of  $AB$ .
    - Find the upper limit and lower limit of  $AD$ .
    - Find the upper limit and lower limit of  $DC$ .
    - Find the upper limit and lower limit of  $AF$ .
  - Is it possible for the actual volume of the prism to be  $21 \text{ m}^3$ ? Explain your answer.



7. The length of a wire is measured as 110 cm, correct to 3 significant figures. The wire is then bent into a square.
- Find the upper limit and lower limit of the length of the side of the square.
  - Find the possible range of the actual area of the square.

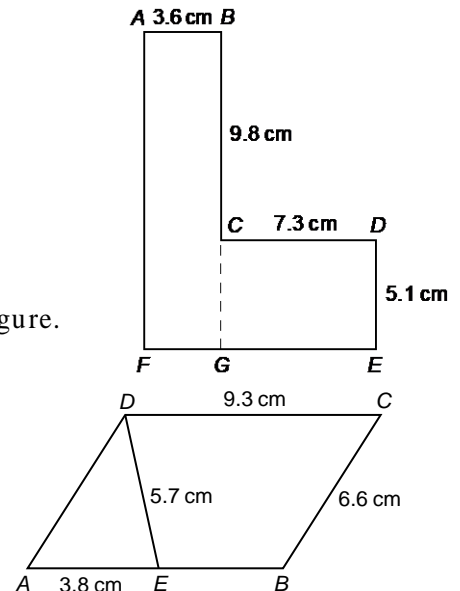
### Challenging Questions

8. In the figure,  $ABCDEFG$  is formed by removing  $\triangle EFG$  from rectangle  $ABCD$ , where all the measurements are correct to 2 significant figures.



- Find the upper limit and lower limit of the actual area of rectangle  $ABCD$ .
- Find the upper limit and lower limit of the actual area of  $\triangle EFG$ .
- Find the possible range of the actual area of  $ABCDEF$ .

- The figure is formed by two rectangles  $ABGF$  and  $CDEG$ , where all the measurements are correct to the nearest 0.1 cm.
  - Write down the maximum absolute error of the measurements.
  - The actual perimeter of the figure is  $x$  cm. Find the range of values of  $x$ .
  - Find the percentage error in calculating the perimeter of the figure. (Give your answer correct to 3 significant figures.)
- The figure shows parallelogram  $ABCD$ .  $AEB$  is a straight line. It is given that all the measurements are correct to 2 significant figures.
  - Find the upper limit and lower limit of  $CD$ .
  - Find the upper limit and lower limit of  $BE$ .
  - Find the possible range of the actual perimeter of  $BCDE$ .
  - Find the percentage error in calculating the perimeter of  $BCDE$ . (Give your answer correct to 3 significant figures.)



## Answers

### Exercise 10A (page 10.1)

- 56.5 cm
- 28.3 cm
- (a) 109.9 cm (b) 123.2 cm
- 12 m
- 14 cm
- $8\pi$  cm
- $11\pi$  cm
- $20\pi$  cm
- 10.5 cm
- 8 cm
- 72.0 cm
- 47.1 cm
- 66.8 cm
- 73.3 cm
- 5 : 3
- 49.8 km/h
- 1768
- (a) 88 cm (b) 24.6 cm
- 1.75 m
- (a) 21 cm (b) 164.0 cm

### Exercise 10B (page 10.3)

- $153.9 \text{ cm}^2$
- $283.5 \text{ cm}^2$
- (a)  $706.5 \text{ cm}^2$  (b)  $498.96 \text{ cm}^2$
- 10.6 cm
- $20\pi \text{ cm}^2$
- $\frac{55\pi}{2} \text{ cm}^2$
- $\frac{145\pi}{8} \text{ cm}^2$
- $447.6 \text{ cm}^2$
- 23.0 m
- $196.3 \text{ cm}^2$
- $132.5 \text{ cm}^2$
- $318.0 \text{ cm}^2$
- $95.0 \text{ cm}^2$
- (a) 9 cm (b)  $9\pi \text{ cm}^2$
- (a) 6.1 (b)  $155.6 \text{ cm}^2$
- (a) 49 : 81 (b)  $73.5 \text{ cm}^2$
- 5.2
- $54.9 \text{ cm}^2$
- (a) 20.1 cm (b)  $93.1 \text{ cm}^2$
- (a) 11.2 cm (b) 49.1%

21. (a)  $\frac{66}{\pi}$  cm  
 (b)  $\left(5 + \frac{33}{\pi}\right)$  cm,  $\left(\frac{33}{\pi} - 5\right)$  cm  
 (c) No

### Exercise 10C (page 10.6)

1. 5.85 cm
2. 29.7 cm
3.  $60.3 \text{ cm}^2$
4.  $44.4 \text{ cm}^2$
5. 9.69 cm
6.  $234^\circ$
7. (a) 12 cm (b) 50.2 cm
8. (a) 6 cm (b)  $300^\circ$
9. (a) 21 cm (b)  $544 \text{ cm}^2$
10. (a) 24.7 cm (b)  $211^\circ$
11. (a) 19.4 cm (b)  $295 \text{ cm}^2$
12. (a) 12.1 cm (b)  $51.0 \text{ cm}^2$
13. (a)  $19.6 \text{ m}^2$  (b)  $65.0 \text{ m}^2$
14. (a) 15 cm (b)  $200\pi \text{ cm}^2$
15. (a) 11.3 cm (b) 59.8 cm  
 (c)  $171 \text{ cm}^2$
16. (a) 55.7 cm (b)  $84.8 \text{ cm}^2$
17.  $282 \text{ cm}^2$
18. (a) 8.66 cm (b)  $240^\circ$   
 (c)  $135 \text{ cm}^2$
19. (a)  $225^\circ$  (b) 8.49 cm  
 (c) 51.2 cm (d)  $182 \text{ cm}^2$

### Exercise 10D (page 10.9)

1.  $320\pi \text{ cm}^3$
2.  $486\pi \text{ cm}^3$
3.  $204\pi \text{ m}^2$
4.  $308\pi \text{ cm}^2$
5. (a) 9.5 cm (b)  $2190 \text{ cm}^2$
6. (a) 7 cm (b)  $448\pi \text{ cm}^3$
7. (a) 11 cm (b)  $864 \text{ cm}^3$
8. (a) 5 cm (b) \$268
9. (a) 18 cm (b)  $1458\pi \text{ cm}^3$
10.  $26.4 \text{ cm}^3$
11.  $62800 \text{ cm}^3$
12.  $434\pi \text{ cm}^2$
13. (a) 2 cm (b) 140%
14. (a) 18 cm (b) Yes
15. (a) 24 cm

- (b) (i) 19.1 cm (ii) 55
16. (a) 6 cm (b)  $726 \text{ cm}^3$
17. (a) Length of  $\widehat{ACB} = 8.20$  cm, length of  $\widehat{DFE} = 10.3$  cm  
 (b)  $204 \text{ cm}^2$
18. (a) 15 cm (b) 2.45 cm
19. (a) 9 m (b) 143 min

### Exercise 10E (page 10.14)

1. 4
2.  $x = 4$ ,  $y = 94.5$
3. 12
4.  $x = 5$ ,  $y = 11.4$
5.  $117 \text{ cm}^2$
6. 36%
7.  $126 \text{ cm}^2$
8. 9 cm
9.  $18.225 \text{ m}^2$
10. 16 cm
11.  $\frac{7}{5}$
12.  $75 \text{ cm}^2$
13. 7 : 8

### Exercise 10F (page 10.16)

1. (a) Upper limit = 2.35 m, lower limit = 2.25 m  
 (b) Upper limit = 1.25 m, lower limit = 1.15 m
2. (a) Upper limit = 13.65 cm, lower limit = 13.55 cm  
 (b) Upper limit = 10.95 cm, lower limit = 10.85 cm  
 (c) Upper limit = 24.6 cm, lower limit = 24.4 cm
3.  $2.25 \text{ cm} \leq PB < 2.27 \text{ cm}$
4. (a) Upper limit = 12.5 cm, lower limit = 11.5 cm  
 (b) Upper limit =  $39.0625\pi \text{ cm}^2$ ,  
 lower limit =  $33.0625\pi \text{ cm}^2$
5. (a) Upper limit = 14.5 cm, lower limit = 13.5 cm  
 (b) Upper limit =  $125.5^\circ$ , lower limit =  $124.5^\circ$   
 (c)  $63.028125\pi \text{ cm}^2$
6. (a) (i) Upper limit = 2.45 m, lower limit = 2.35 m  
 (ii) Upper limit = 2.25 m, lower limit = 2.15 m  
 (iii) Upper limit = 3.05 m, lower limit = 2.95 m  
 (iv) Upper limit = 3.25 m, lower limit = 3.15 m  
 (b) No
7. (a) Upper limit = 27.625 cm, lower limit = 27.375 cm  
 (b)  $749.390625 \text{ cm}^2 \leq \text{Actual area of the square} < 763.140625 \text{ cm}^2$
8. (a) Upper limit =  $428.75 \text{ cm}^2$ , lower limit =  $387.75 \text{ cm}^2$   
 (b) Upper limit =  $60.375 \text{ cm}^2$ , lower limit =  $49.875 \text{ cm}^2$   
 (c)  $327.375 \text{ cm}^2 \leq \text{Actual area of } ABCDEFG < 378.875 \text{ cm}^2$
9. (a) 0.05 cm

- (b)  $51.2 \leq x < 52$
  - (c) 0.775%
10. (a) Upper limit = 9.35 cm, lower limit = 9.25 cm
- (b) Upper limit = 5.6 cm, lower limit = 5.4 cm
  - (c)  $26.85 \text{ cm} \leq \text{Actual perimeter of } BCDE < 27.35 \text{ cm}$
  - (d) 0.923%

## English Version

### 12 Trigonometric Ratios



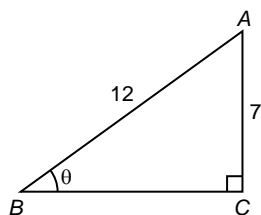
## Exercise 12A



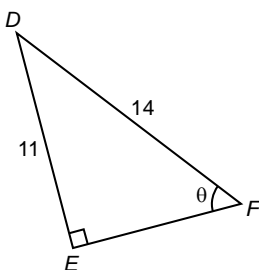
### Fundamental Questions

Find the value of  $\sin \theta$  in each of the following figures. (1 – 3)

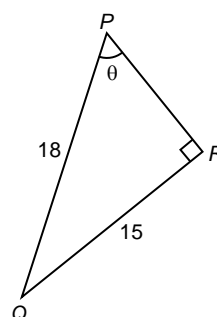
1.



2.

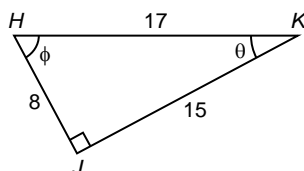


3.

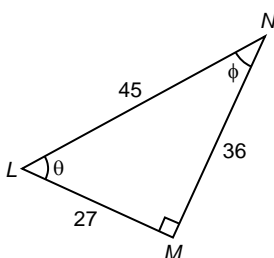


Find the values of  $\sin \theta$  and  $\sin \phi$  in each of the following figures. (4 – 6)

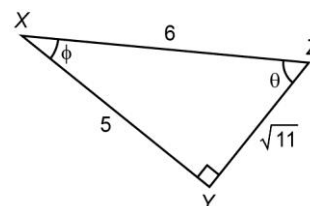
4.



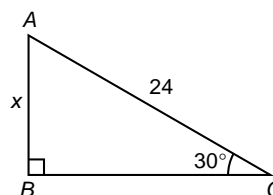
5.



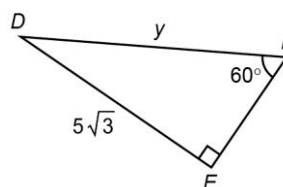
6.



7. It is given that  $\sin 30^\circ = 0.5$ . Find  $x$  in the figure.



8. It is given that  $\sin 60^\circ = \frac{\sqrt{3}}{2}$ . Find  $y$  in the figure.



### Consolidation Questions

9. Find the values of the following. (Give your answers correct to 3 significant figures.)

(a)  $\sin 23^\circ$

(b)  $2\sin 35^\circ$

(c)  $\frac{5}{\sin 16^\circ}$

(d)  $\sin 74^\circ + 1.5$

(e)  $\sin 66^\circ + \sin 34^\circ$

(f)  $\sin 86^\circ - 2\sin 12^\circ$

(g)  $\frac{\sin 28^\circ}{\sin 62^\circ}$

(h)  $\frac{2\sin 20^\circ - \sin 40^\circ}{\sin 10^\circ}$

10. Find  $\theta$  in the following. (Give your answers correct to 1 decimal place if necessary.)

(a)  $\sin \theta = 0.2$

(b)  $\sin \theta = \frac{12}{55}$

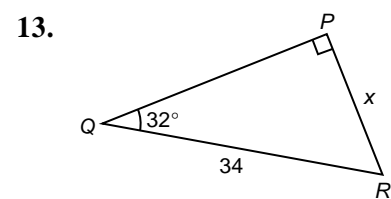
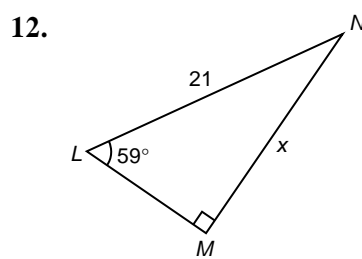
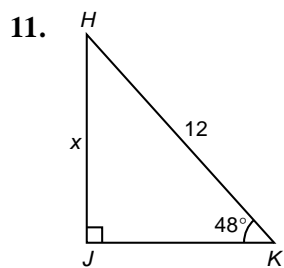
(c)  $\sin \theta = \frac{\sqrt{2}}{5}$

(d)  $5 \sin \theta = 3$

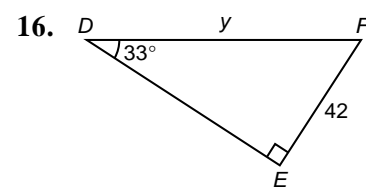
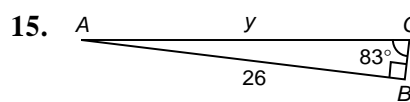
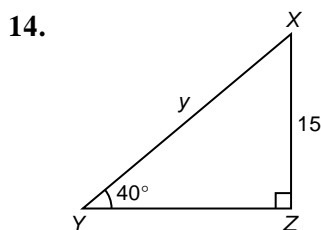
(e)  $\sin \theta = \sin 10^\circ \sin 80^\circ$

(f)  $\sin \theta = \frac{\sin 36^\circ}{2 \sin 18^\circ}$

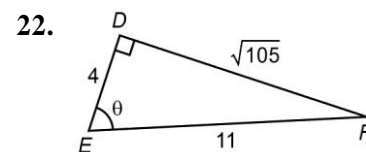
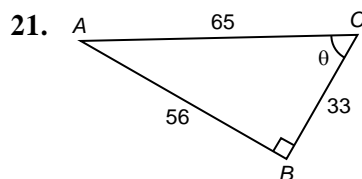
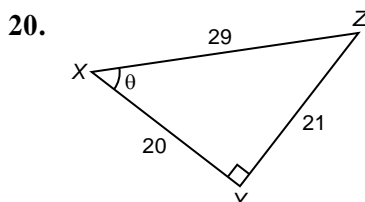
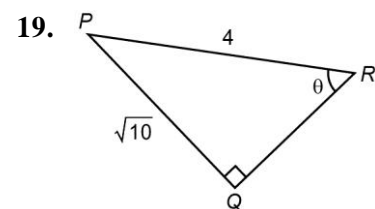
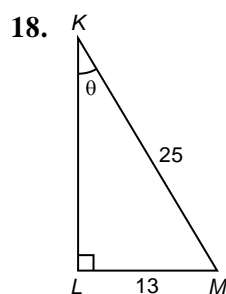
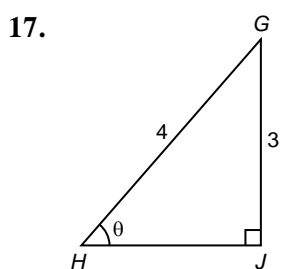
Find  $x$  in each of the following figures correct to 3 significant figures. (11 – 13)



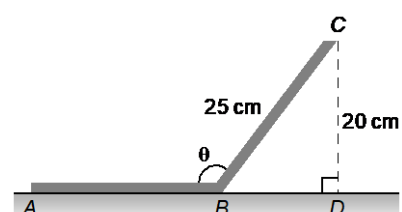
Find  $y$  in each of the following figures correct to 1 decimal place. (14 – 16)



Find  $\theta$  in each of the following figures correct to the nearest degree. (17 – 22)



23. A notebook computer is opened as shown in the figure. Find  $\theta$ . (Give your answer correct to 3 significant figures.)

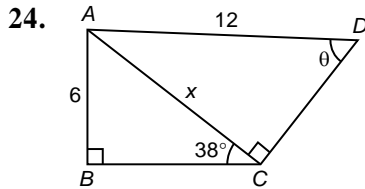




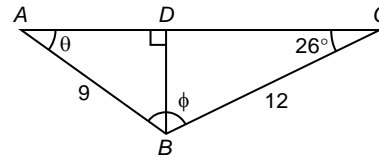


## Challenging Questions

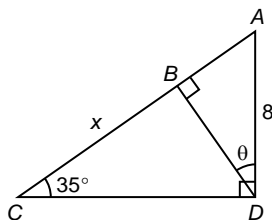
Find the unknowns in the following figures. (Give your answers correct to 3 significant figures if necessary.) (24 – 27)



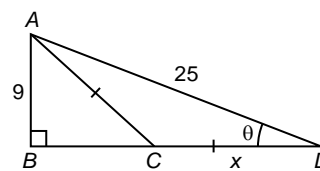
25.  $ADC$  is a straight line.



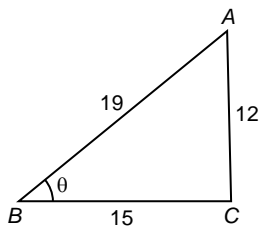
26.  $ABC$  is a straight line.



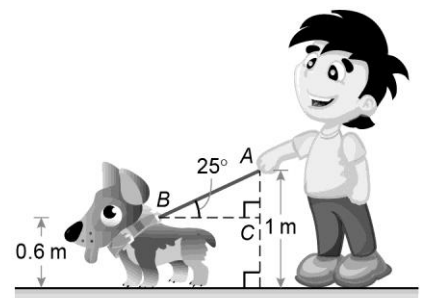
27.  $BCD$  is a straight line.



28. The figure shows  $\triangle ABC$ . Alvin claims that  $\sin \theta = \frac{AC}{AB}$ . Do you agree? Explain your answer.



29. A boy walks with his dog in the figure. He holds a rope at  $A$  and the rope is connected to the dog's collar at  $B$ . The rope is stretched tight and it makes an angle of  $25^\circ$  with the horizontal. It is given that  $A$  and  $B$  are 1 m and 0.6 m above the horizontal ground respectively. Find the length of the rope  $AB$ . (Give your answer correct to 3 significant figures.)

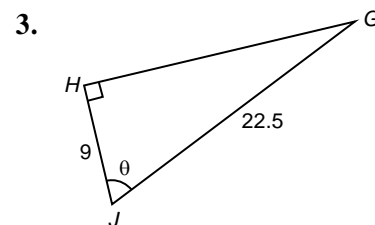
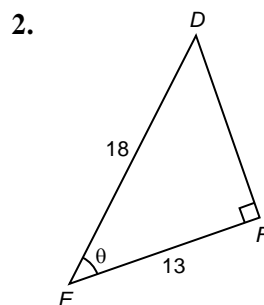
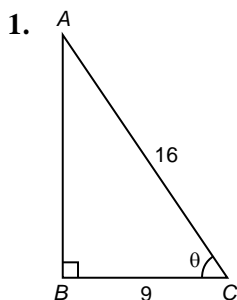


## Exercise 12B



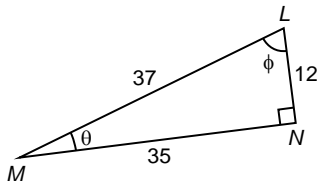
### Fundamental Questions

Find the value of  $\cos \theta$  in each of the following figures. (1 – 3)

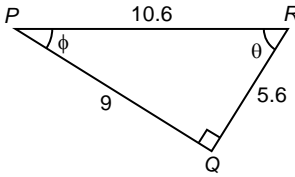


Find the values of  $\cos\theta$  and  $\cos\phi$  in each of the following figures. (4 – 6)

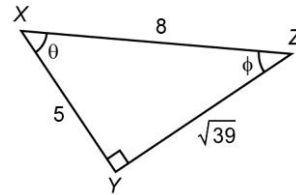
4.



5.



6.



### Consolidation Questions

7. Find the values of the following. (Give your answers correct to 3 significant figures.)

(a)  $\cos 17^\circ$

(b)  $3\cos 8^\circ$

(c)  $\frac{9}{\cos 74^\circ}$

(d)  $\cos 36^\circ - 0.2$

(e)  $\cos 10^\circ - \cos 50^\circ$

(f)  $2\cos 28^\circ + 3\cos 53^\circ$

(g)  $\frac{\cos 44^\circ}{3\cos 22^\circ}$

(h)  $\frac{\cos 5^\circ}{3\cos 70^\circ - 2\cos 82^\circ}$

8. Find  $\theta$  in the following. (Give your answers correct to 1 decimal place if necessary.)

(a)  $\cos\theta = 0.6$

(b)  $\cos\theta = \frac{23}{37}$

(c)  $\cos\theta = \frac{1}{\sqrt{6}}$

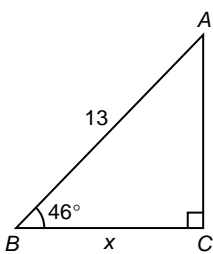
(d)  $2\cos\theta = \sqrt{3}$

(e)  $\cos\theta = 2\cos 50^\circ \cos 42^\circ$

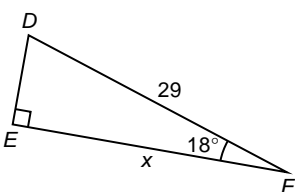
(f)  $\cos\theta = \frac{2\cos 85^\circ}{\cos 15^\circ}$

Find  $x$  in each of the following figures correct to 3 significant figures. (9 – 11)

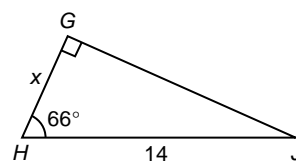
9.



10.

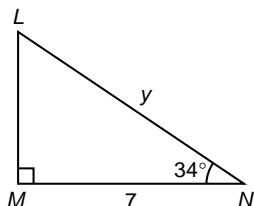


11.

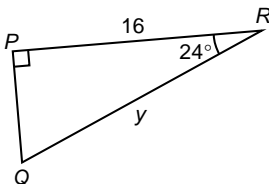


Find  $y$  in each of the following figures correct to 1 decimal place. (12 – 14)

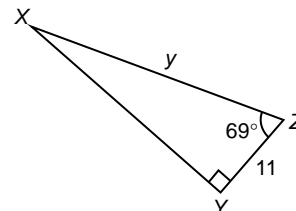
12.



13.

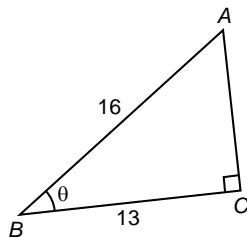


14.

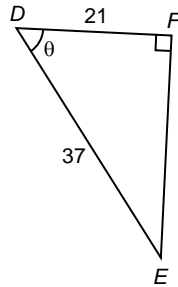


Find  $\theta$  in each of the following figures correct to the nearest degree. (15 – 17)

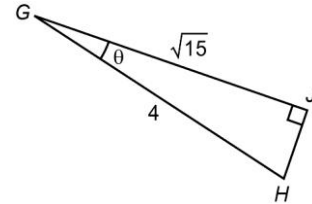
15.



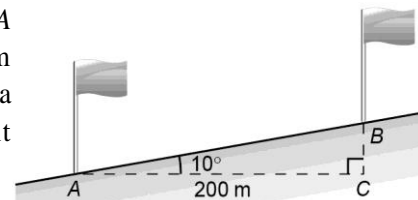
16.



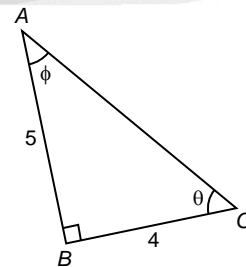
17.



18. The figure shows two flagpoles standing vertically at points  $A$  and  $B$  on a slope, where the horizontal distance between them is 200 m. Find the time taken by Marco to walk from  $A$  to  $B$  at a speed of 3 m/s. (Give your answer correct to 3 significant figures.)



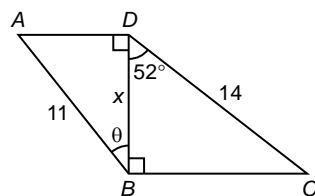
19. In the figure,  $\triangle ABC$  is a right-angled triangle. Without finding  $\theta$  and  $\phi$ , find the value of  $\frac{\cos \theta}{\cos \phi}$ .



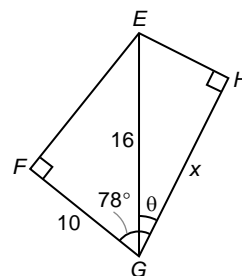
### Challenging Questions

Find the unknowns in the following figures. (Give your answers correct to 3 significant figures.) (20 – 23)

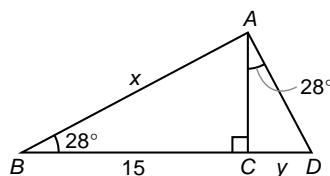
20.



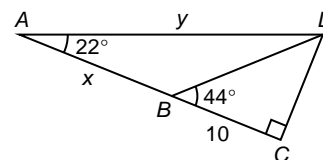
21.



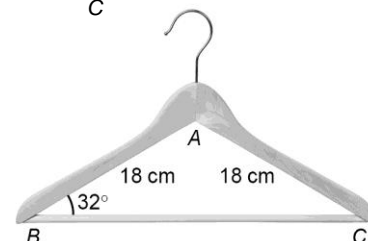
22.  $BCD$  is a straight line.



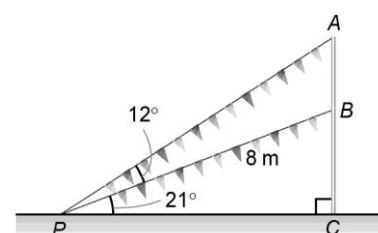
23.  $ABC$  is a straight line.



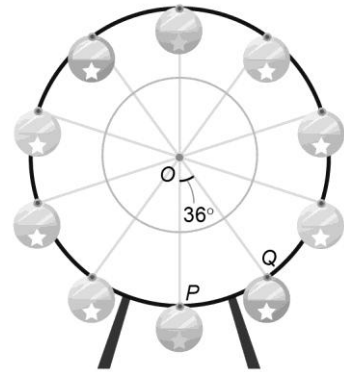
24. The figure shows a hanger, where  $AB = AC = 18$  cm and  $\angle ABC = 32^\circ$ . Find the length of  $BC$ . (Give your answer correct to 3 significant figures.)



25. In the figure, two ribbons  $AP$  and  $BP$  connect a rod  $ABC$  to the ground at  $P$ . By how much is the length of  $AP$  longer than that of  $BP$ ? (Give your answer correct to 3 significant figures.)



26. The figure shows a Ferris wheel with centre  $O$  and the radius of 20 m.  $P$  and  $Q$  are the highest points of two cabins of the Ferris wheel, where  $P$  is vertically below the centre  $O$  and  $\angle POQ = 36^\circ$ . If  $P$  is 10 m above the ground, find the height of  $Q$  above the ground. (Give your answer correct to 3 significant figures.)

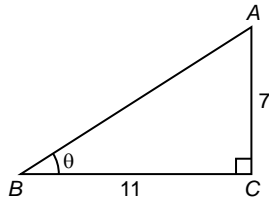


## Exercise 12C

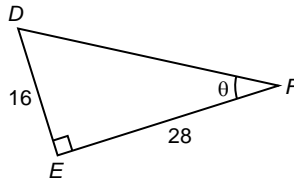
### Fundamental Questions

Find the value of  $\tan \theta$  in each of the following figures. (1 – 3)

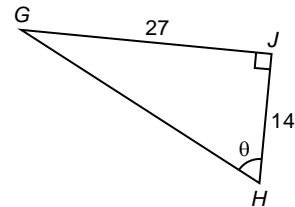
1.



2.

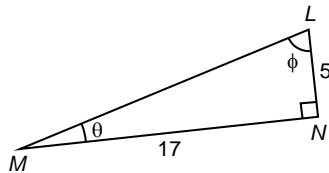


3.

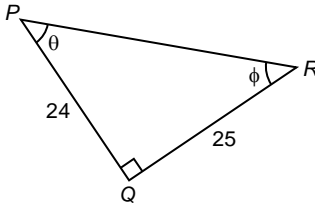


Find the values of  $\tan \theta$  and  $\tan \phi$  in each of the following figures. (4 – 6)

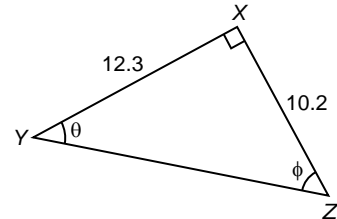
4.



5.



6.



### Consolidation Questions

7. Find the values of the following. (Give your answers correct to 3 significant figures.)

(a)  $\tan 54^\circ$

(b)  $\frac{\tan 22^\circ}{4}$

(c)  $\frac{12}{\tan 35^\circ}$

(d)  $\tan 38^\circ \tan 67^\circ$

(e)  $\tan 80^\circ - \tan 70^\circ$

(f)  $3 \tan 22^\circ + 2 \tan 6^\circ$

(g)  $\frac{\tan 25^\circ}{5 \tan 15^\circ}$

(h)  $\frac{\tan 43^\circ - \tan 21^\circ}{\tan 10^\circ}$

8. Find  $\theta$  in the following. (Give your answers correct to 1 decimal place.)

(a)  $\tan \theta = 1.7$

(b)  $\tan \theta = \frac{15}{28}$

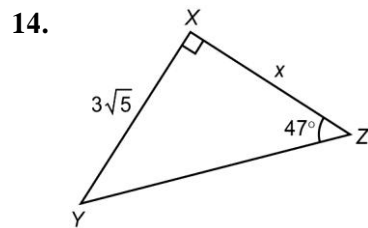
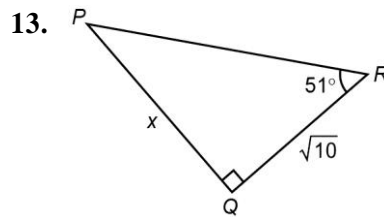
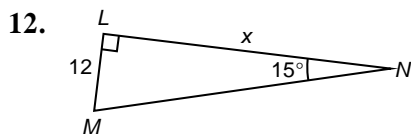
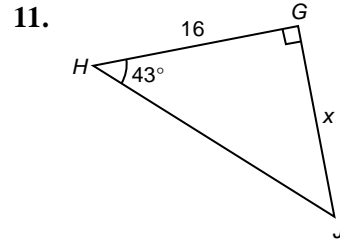
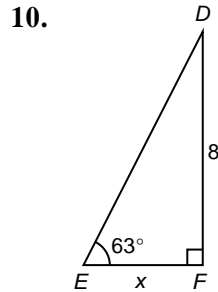
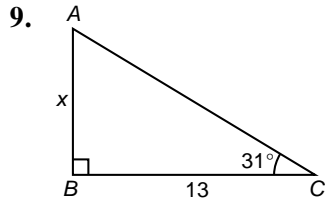
(c)  $\tan \theta = \frac{4}{\sqrt{3}}$

(d)  $4 \tan \theta = 3\sqrt{2}$

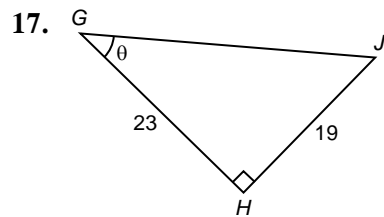
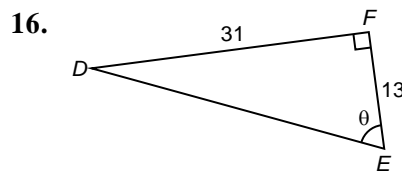
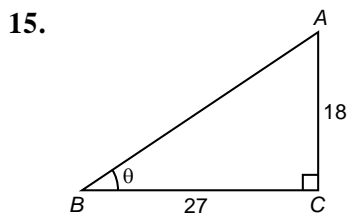
(e)  $\tan \theta = 4 \tan 37^\circ \tan 74^\circ$

(f)  $\tan \theta = \frac{\tan 84^\circ}{7 \tan 12^\circ}$

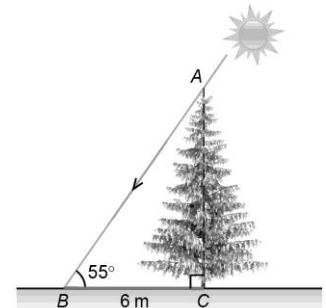
Find  $x$  in each of the following figures correct to 3 significant figures. (9 – 14)



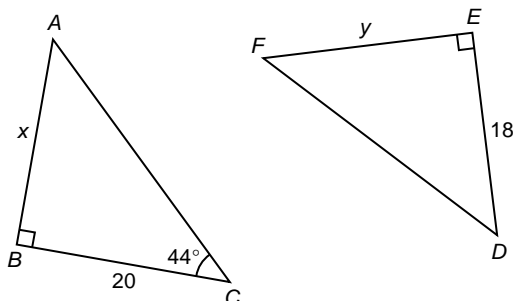
Find  $\theta$  in each of the following figures correct to the nearest degree. (15 – 17)



18. In the figure, the sun rays make an angle of  $55^\circ$  with the horizontal ground, and the tree casts a shadow  $BC$  of 6 m long. Find the height of the tree. (Give your answer correct to 3 significant figures.)



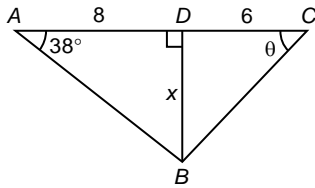
19. In the figure,  $\triangle ABC \sim \triangle DEF$ . Find  $x$  and  $y$  correct to 3 significant figures.



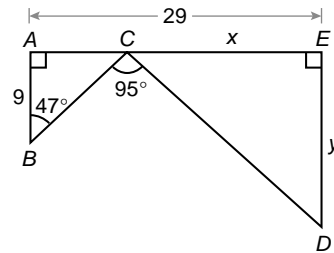
### Challenging Questions

Find the unknowns in the following figures. (Give your answers correct to 3 significant figures if necessary.) (20 – 23)

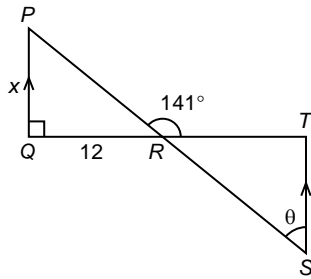
20.  $ADC$  is a straight line.



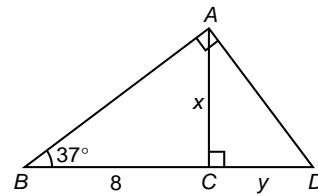
21.  $ACE$  is a straight line.



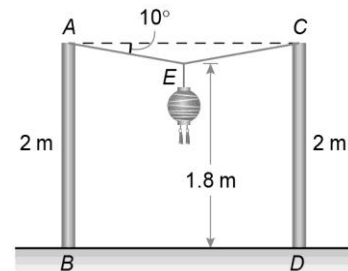
22.  $PRS$  and  $QRT$  are straight lines.



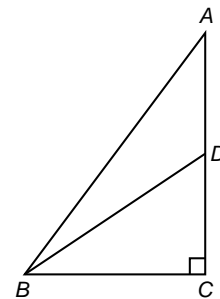
23.  $BCD$  is a straight line.



24. In the figure, the rods  $AB$  and  $CD$  are both 2 m high. A lantern is hung at point  $E$  on the rope joining  $A$  and  $C$ , where  $AE = CE$ . It is given that  $AE$  makes an angle of  $10^\circ$  with  $AC$  and  $E$  is 1.8 m above the ground. Find the distance between the rods  $AB$  and  $CD$ . (Give your answer correct to 3 significant figures.)



★ 25. In the figure,  $\triangle ABC$  is a right-angled triangle.  $D$  is a point on  $AC$  such that  $AD:DC:BC = 2:2:3$ . Judy claims that  $\angle ABD = \angle DBC$ . Do you agree? Explain your answer.



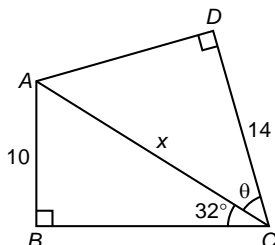
## Exercise 12D

[In this exercise, give your answers correct to 3 significant figures if necessary.]

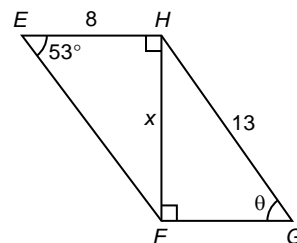
### Fundamental Questions

Find the unknowns in the following figures. (1 – 6)

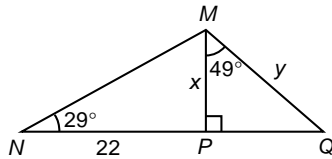
1.



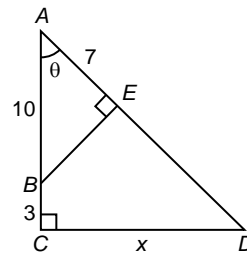
2.



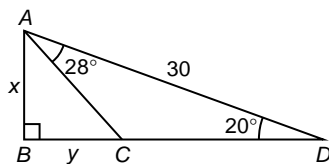
3.  $NPQ$  is a straight line.



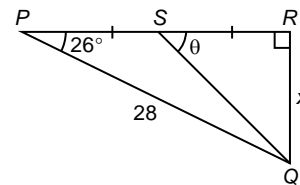
4.  $ABC$  and  $AED$  are straight lines.



5.  $BCD$  is a straight line.

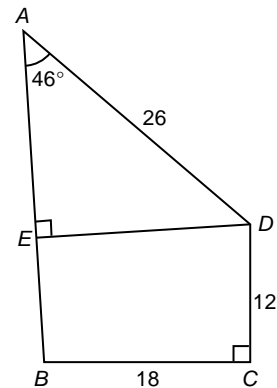


6.  $PSR$  is a straight line.

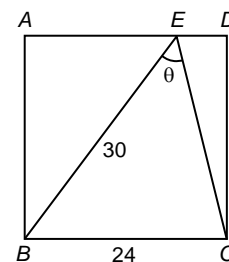


### Consolidation Questions

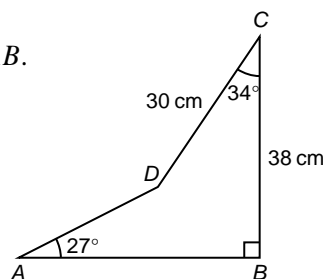
7. In the figure,  $ABCD$  is a quadrilateral.  $E$  is a point on  $AB$  such that  $AB \perp DE$ . Find  $\angle CDE$ .



8. In the figure,  $ABCD$  is a square.  $E$  is a point on  $AD$ . Find  $\theta$ .



9. In the figure,  $ABCD$  is a quadrilateral. Find  $AB$ .

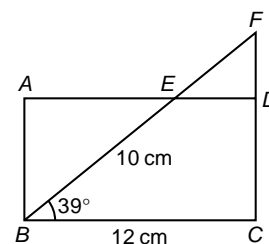


10. In the figure,  $ABCD$  is a rectangle.  $AED$ ,  $BEF$  and  $FDC$  are straight lines.

(a) Find  $AB$  and  $AE$ .

(b) Find  $FD$ .

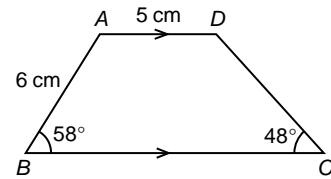
- (c) Tina claims that the sum of the areas of  $\triangle ABE$  and  $\triangle DEF$  is smaller than half of the area of  $ABCD$ . Do you agree?



Explain your answer.

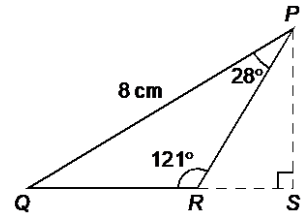
11. In the figure,  $ABCD$  is a trapezium, where  $AD \parallel BC$ .

- (a) Find the length of  $BC$ .  
(b) Find the area of the trapezium  $ABCD$ .



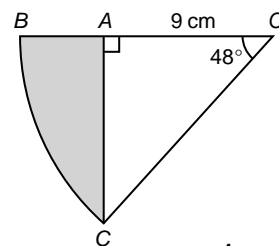
12. In the figure,  $S$  is a point on  $QR$  produced such that  $PS \perp QS$ .

- (a) Find the length of  $PS$ .  
(b) Find the length of  $QR$ .  
(c) Find the area of  $\triangle PQR$ .  
(d) Find the perpendicular distance from  $R$  to  $PQ$ .

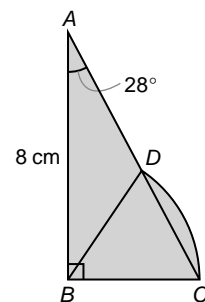


13. In the figure,  $OBC$  is a sector.  $A$  is a point on  $OB$  such that  $AC \perp OB$ . It is given that  $OA = 9$  cm and  $\angle BOC = 48^\circ$ .

- (a) Find the radius of the sector  $OBC$ .  
(b) Find the area of the shaded region.

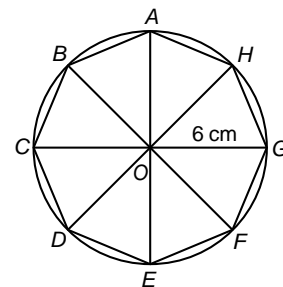


14. In the figure,  $\triangle ABC$  is a right-angled triangle, where  $\angle A = 28^\circ$ .  $D$  is a point on  $AC$  such that  $BCD$  is a sector. Find the area of the figure.



15. In the figure,  $O$  is the centre of a circle of radius 6 cm.  $A, B, C, D, E, F, G$  and  $H$  are points on the circle such that  $ABCDEFGH$  is a regular octagon.

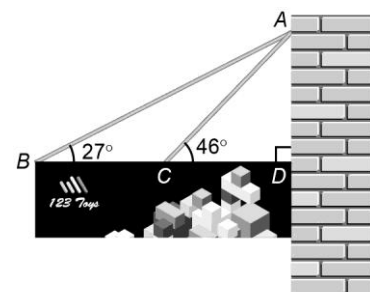
- (a) Find the perimeter of the octagon.  
(b) Find the area of the octagon.



### Challenging Questions

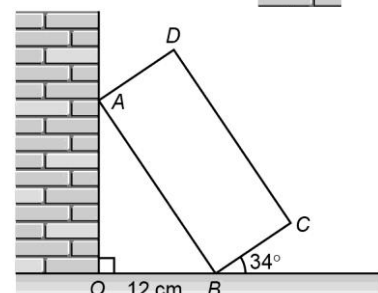
16. In the figure, a rectangular advertising board is hung on the vertical wall by two rods  $AB$  and  $AC$ . It is given that the total length of the two rods is 8 m.

- (a) Find the height of  $A$  above the advertising board.  
(b) Find the length  $BD$  of the advertising board.



17. In the figure, a rectangular block leans against the vertical wall, where  $BC$  makes an angle of  $34^\circ$  with the horizontal ground. It is given that the height of  $D$  above the ground is 23 cm.

- (a) Find the lengths of  $AB$  and  $AD$ .





(b) Find the distance of  $C$  from the wall.

- ★ 18. Figure I shows a piece of rectangular paper. The paper is folded as shown in Figure II. Let  $AE = x$  cm.
- Find the length of  $BF$ .
  - Find the value of  $x$ .
  - Which one of  $\angle FEC$  and  $\angle FCB$  is greater? Explain your answer.

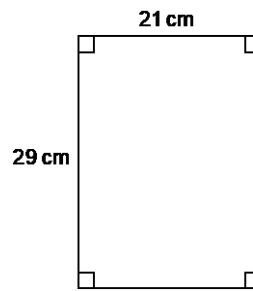


Figure I

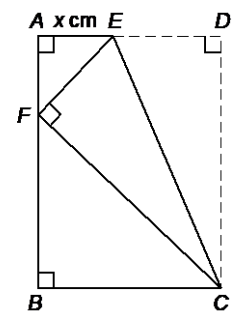


Figure II

## Answers

### Exercise 12A (page 12.1)

- $\frac{7}{12}$
- $\frac{11}{14}$
- $\frac{5}{6}$
- $\sin \theta = \frac{8}{17}, \sin \phi = \frac{15}{17}$
- $\sin \theta = \frac{4}{5}, \sin \phi = \frac{3}{5}$
- $\sin \theta = \frac{5}{6}, \sin \phi = \frac{\sqrt{11}}{6}$
- 12
- 10
- (a) 0.391  
(b) 1.15  
(c) 18.1  
(d) 2.46  
(e) 1.47  
(f) 0.582  
(g) 0.532  
(h) 0.238
- (a)  $11.5^\circ$   
(b)  $12.6^\circ$   
(c)  $16.4^\circ$   
(d)  $36.9^\circ$   
(e)  $9.8^\circ$   
(f)  $72^\circ$
- 8.92
- 18.0
- 18.0
- 23.3
- 26.2
- 77.1
- $49^\circ$

- $31^\circ$
- $52^\circ$
- $46^\circ$
- $59^\circ$
- $69^\circ$
- $127^\circ$
- $x = 9.75, \theta = 54.3^\circ$
- $\theta = 35.8^\circ, \phi = 118^\circ$
- $\theta = 35^\circ, x = 9.36$
- $\theta = 21.1^\circ, x = 13.4$
- No
- 0.946 m

### Exercise 12B (page 12.4)

- $\frac{9}{16}$
- $\frac{13}{18}$
- $\frac{2}{5}$
- $\cos \theta = \frac{35}{37}, \cos \phi = \frac{12}{37}$
- $\cos \theta = \frac{28}{53}, \cos \phi = \frac{45}{53}$
- $\cos \theta = \frac{5}{8}, \cos \phi = \frac{\sqrt{39}}{8}$
- (a) 0.956  
(b) 2.97  
(c) 32.7  
(d) 0.609  
(e) 0.342  
(f) 3.57  
(g) 0.259  
(h) 1.33
- (a)  $53.1^\circ$   
(b)  $51.6^\circ$   
(c)  $65.9^\circ$   
(d)  $30^\circ$

- (e)  $17.2^\circ$   
 (f)  $79.6^\circ$
9. 9.03  
 10. 27.6  
 11. 5.69  
 12. 8.4  
 13. 17.5  
 14. 30.7  
 15.  $36^\circ$   
 16.  $55^\circ$   
 17.  $14^\circ$   
 18. 67.7 s  
 19.  $\frac{4}{5}$   
 20.  $x = 8.62$ ,  $\theta = 38.4^\circ$   
 21.  $\theta = 26.7^\circ$ ,  $x = 14.3$   
 22.  $x = 17.0$ ,  $y = 4.24$   
 23.  $x = 13.9$ ,  $y = 25.8$   
 24. 30.5 cm  
 25. 0.905 m  
 26. 13.8 m

### Exercise 12C (page 12.7)

1.  $\frac{7}{11}$   
 2.  $\frac{4}{7}$   
 3.  $\frac{27}{14}$   
 4.  $\tan \theta = \frac{5}{17}$ ,  $\tan \phi = \frac{17}{5}$   
 5.  $\tan \theta = \frac{25}{24}$ ,  $\tan \phi = \frac{24}{25}$   
 6.  $\tan \theta = \frac{34}{41}$ ,  $\tan \phi = \frac{41}{34}$   
 7. (a) 1.38  
 (b) 0.101  
 (c) 17.1  
 (d) 1.84  
 (e) 2.92  
 (f) 1.42  
 (g) 0.348  
 (h) 3.11  
 8. (a)  $59.5^\circ$   
 (b)  $28.2^\circ$   
 (c)  $66.6^\circ$   
 (d)  $46.7^\circ$   
 (e)  $84.6^\circ$   
 (f)  $81.1^\circ$   
 9. 7.81  
 10. 4.08  
 11. 14.9

12. 44.8  
 13. 3.91  
 14. 6.26  
 15.  $34^\circ$   
 16.  $67^\circ$   
 17.  $40^\circ$   
 18. 8.57 m  
 19.  $x = 19.3$ ,  $y = 18.6$   
 20.  $x = 6.25$ ,  $\theta = 46.2^\circ$   
 21.  $x = 19.3$ ,  $y = 17.4$   
 22.  $x = 9.72$ ,  $\theta = 51^\circ$   
 23.  $x = 6.03$ ,  $y = 4.54$   
 24. 2.27 m  
 25. No

### Exercise 12D (page 12.11)

1.  $x = 18.9$ ,  $\theta = 42.1^\circ$   
 2.  $x = 10.6$ ,  $\theta = 54.8^\circ$   
 3.  $x = 12.2$ ,  $y = 18.6$   
 4.  $\theta = 45.6^\circ$ ,  $x = 13.3$   
 5.  $x = 10.3$ ,  $y = 9.24$   
 6.  $x = 12.3$ ,  $\theta = 44.3^\circ$   
 7.  $86.5^\circ$   
 8.  $50.9^\circ$   
 9. 42.5 cm  
 10. (a)  $AB = 6.29$  cm,  $AE = 7.77$  cm  
 (b) 3.42 cm  
 (c) Yes  
 11. (a) 12.8 cm  
 (b)  $45.2 \text{ cm}^2$   
 12. (a) 4.12 cm  
 (b) 4.38 cm  
 (c)  $9.03 \text{ cm}^2$   
 (d) 2.26 cm  
 13. (a) 13.5 cm  
 (b)  $30.8 \text{ cm}^2$   
 14.  $18.4 \text{ cm}^2$   
 15. (a) 36.7 cm  
 (b)  $102 \text{ cm}^2$   
 16. (a) 2.23 m  
 (b) 4.37 m  
 17. (a)  $AB = 21.5$  cm,  $AD = 9.32$  cm  
 (b) 19.7 cm  
 18. (a) 20 cm  
 (b)  $\frac{60}{7}$   
 (c)  $\angle FEC$